

Secret JPEG Image Sharing

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Motivations

- Intensive image exchanges over social networks.
- Standard compression format is JPEG.

How can we ensure JPEG image security ?



G.K. Wallace, "The JPEG still picture compression standard." *Communications of the ACM* 34.4 (1991): 30-44.



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How can we ensure JPEG image security ?

- Crypto-compression is often used **BUT** depends on a secret key.

Solution: Using secret sharing jointly to JPEG compression.



G.K. Wallace, "The JPEG still picture compression standard." *Communications of the ACM* 34.4 (1991): 30-44.

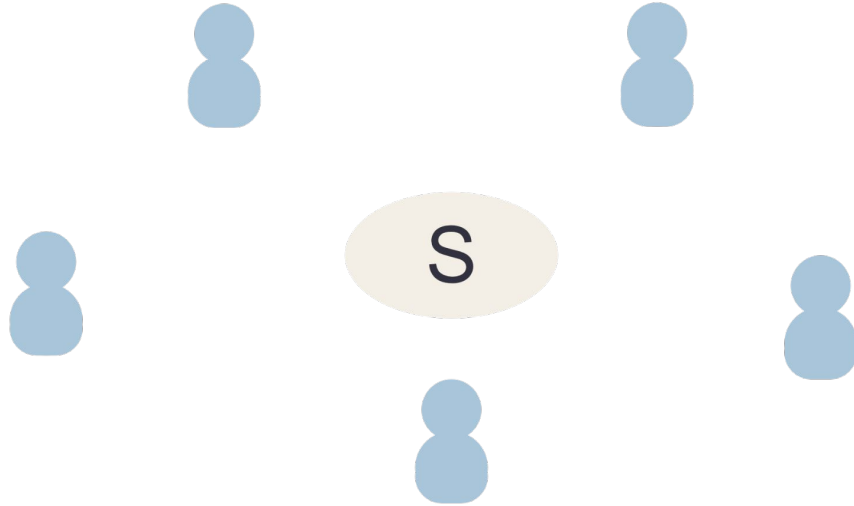


Secret sharing

- Number of users: n

- For instance:

$$n = 5$$



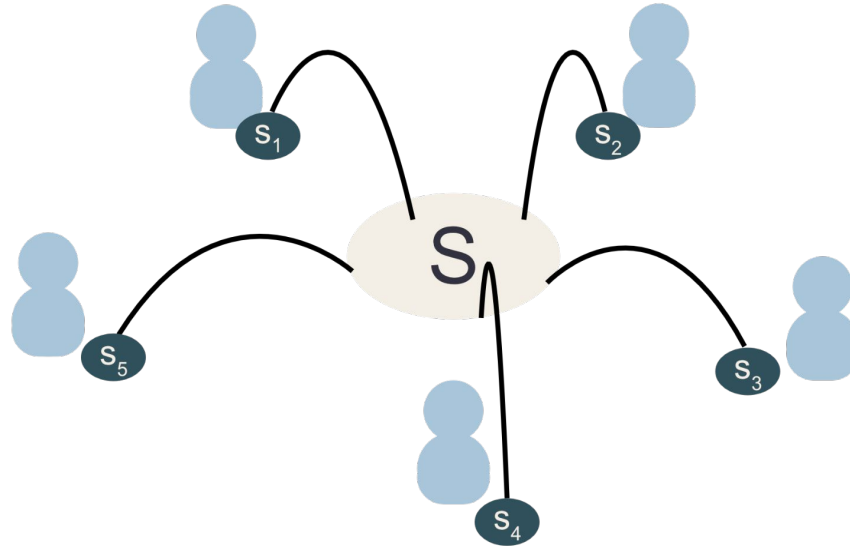
A. Shamir, "How to share a secret." *Communications of the ACM* 22.11 (1979): 612-613.

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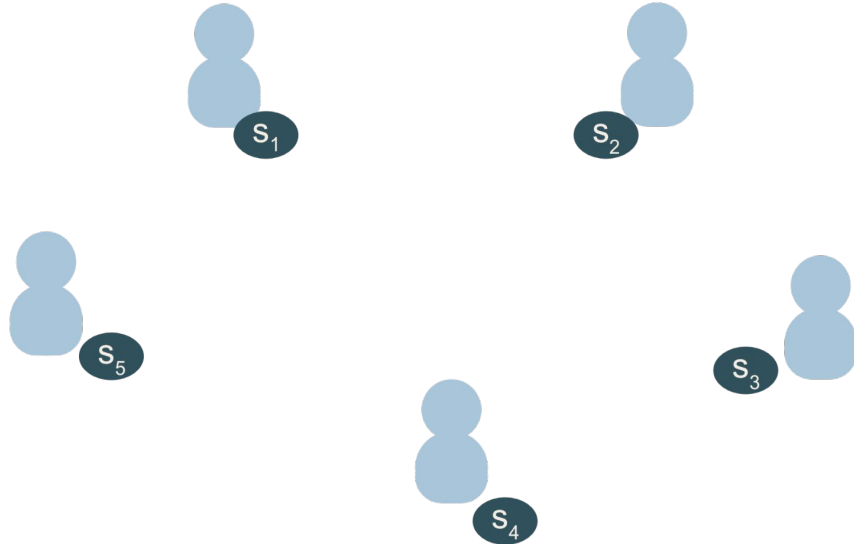
Secret sharing

- Number of users: n
- Threshold: k

- For instance:

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$$k = 3$$



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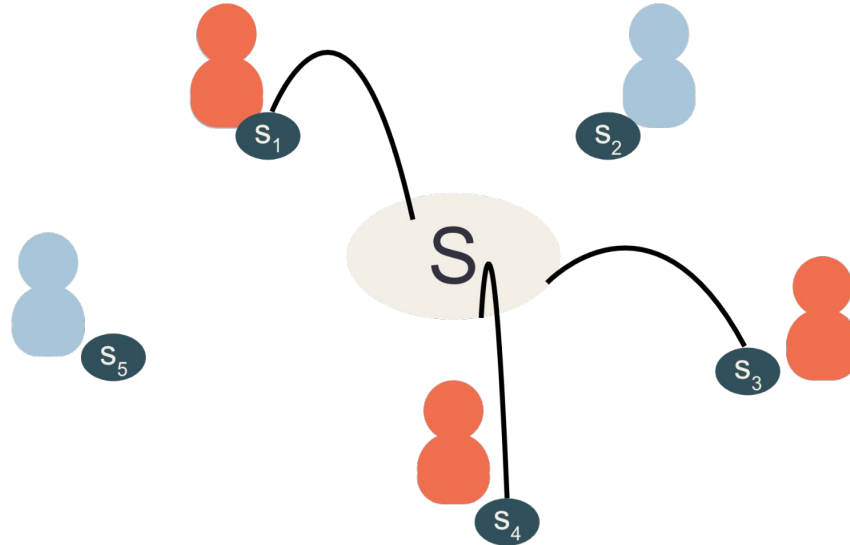
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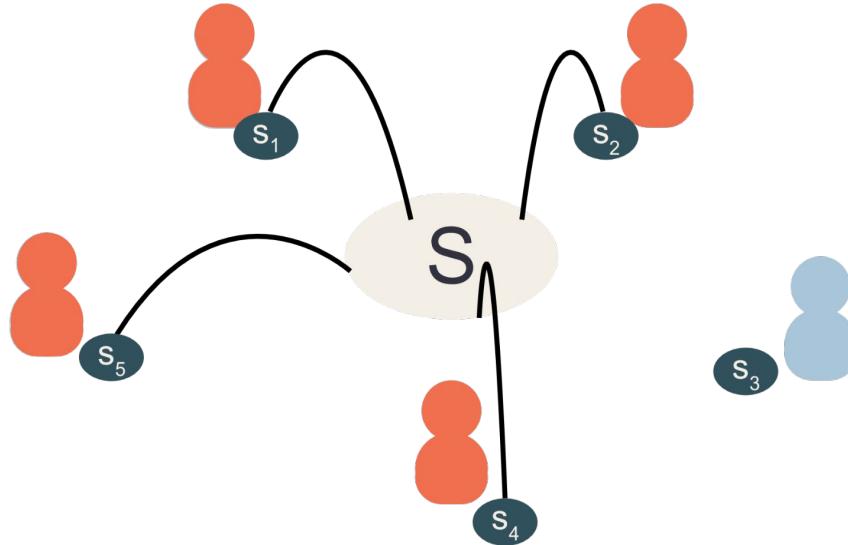
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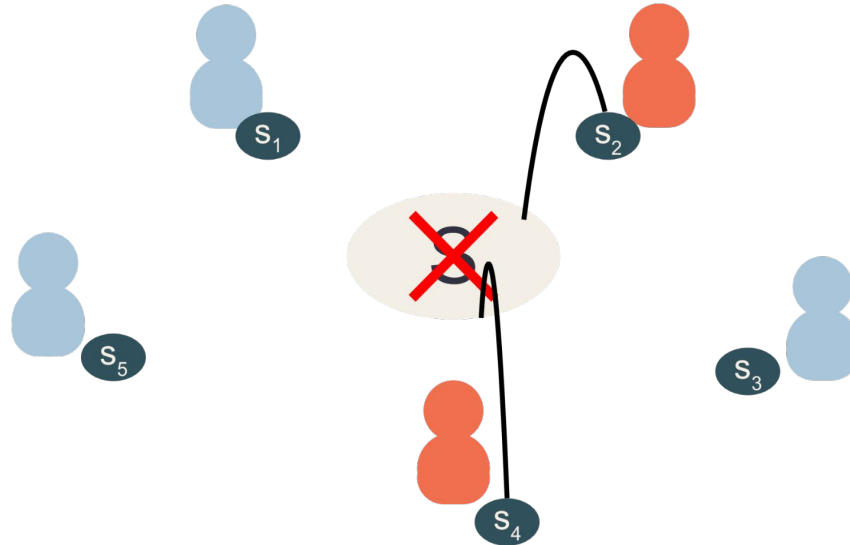
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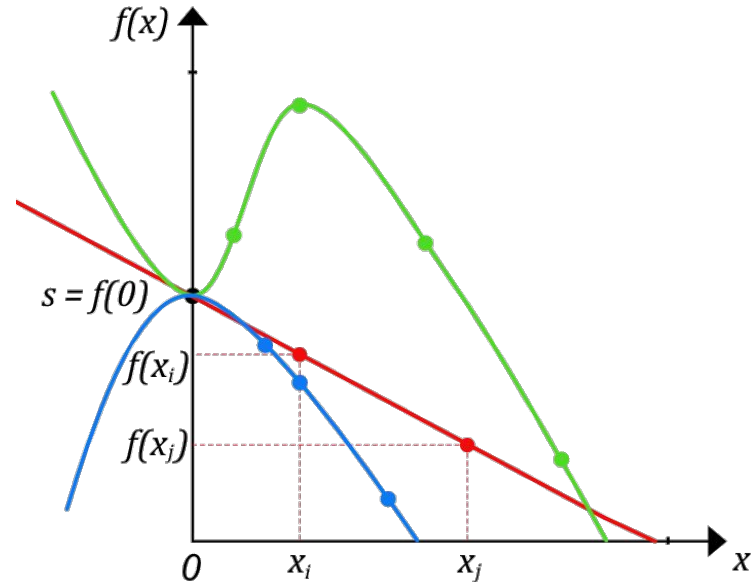
Secret sharing

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How does it work?

- Secret value to share: s
- Finite field
- Based on polynomial interpolation:

$$f(x) = \left(\sum_{l=1}^{k-1} a_l x^l \right) + s$$

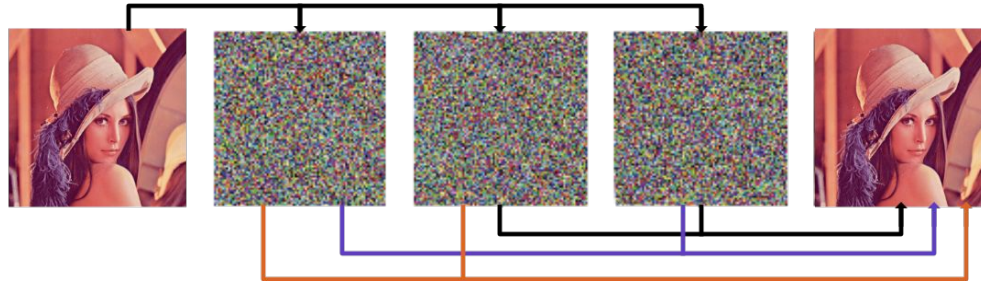


A. Shamir, "How to share a secret." *Communications of the ACM* 22.11 (1979): 612-613.

Secret image sharing

- Sharing pixel values.
- Each user receives a shared image.

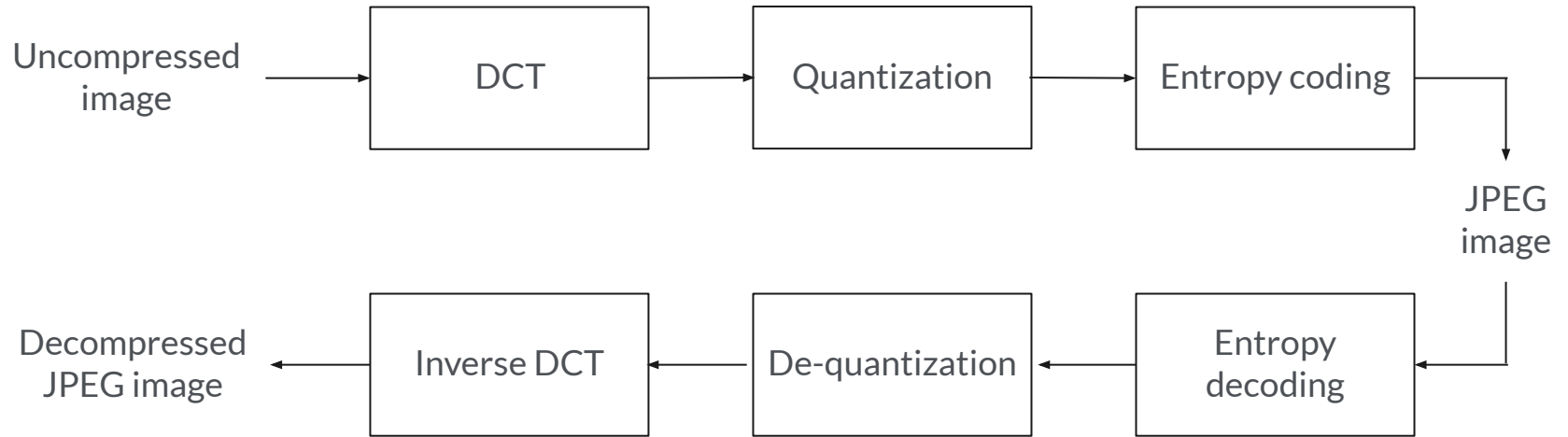
How to extend this principle to JPEG images?



C. C. Thien and J. Lin, "Secret image sharing." *Computers & Graphics* 26.5 (2002): 765-770.

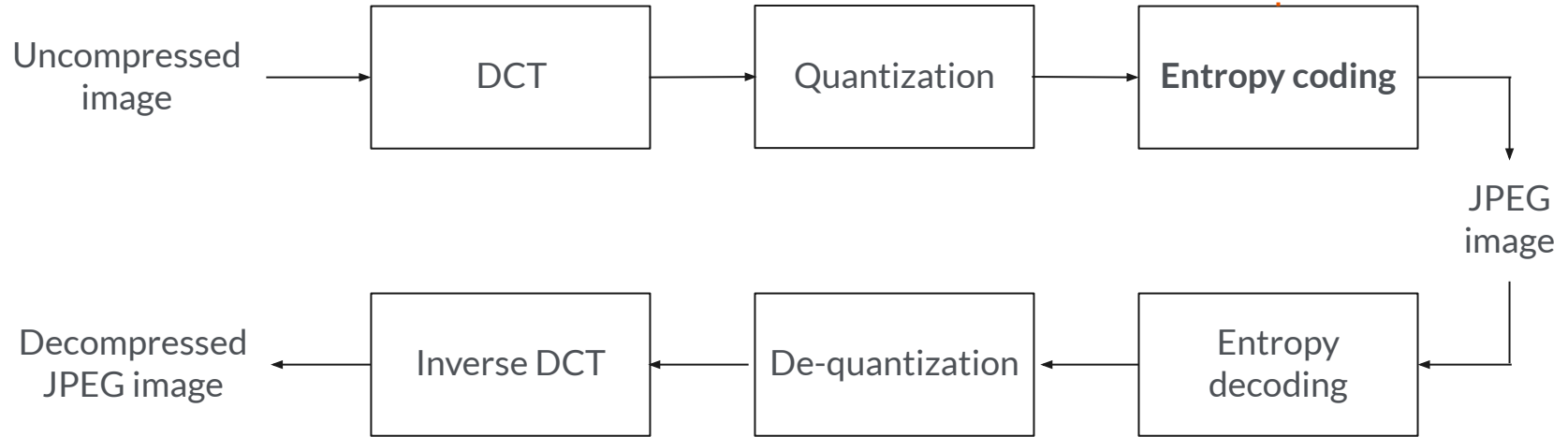


JPEG compression



JPEG compression

$$\text{Quantized AC frequency coefficient} \\ F'(u,v) = (H_{F'(u,v)} A_{F'(u,v)})$$

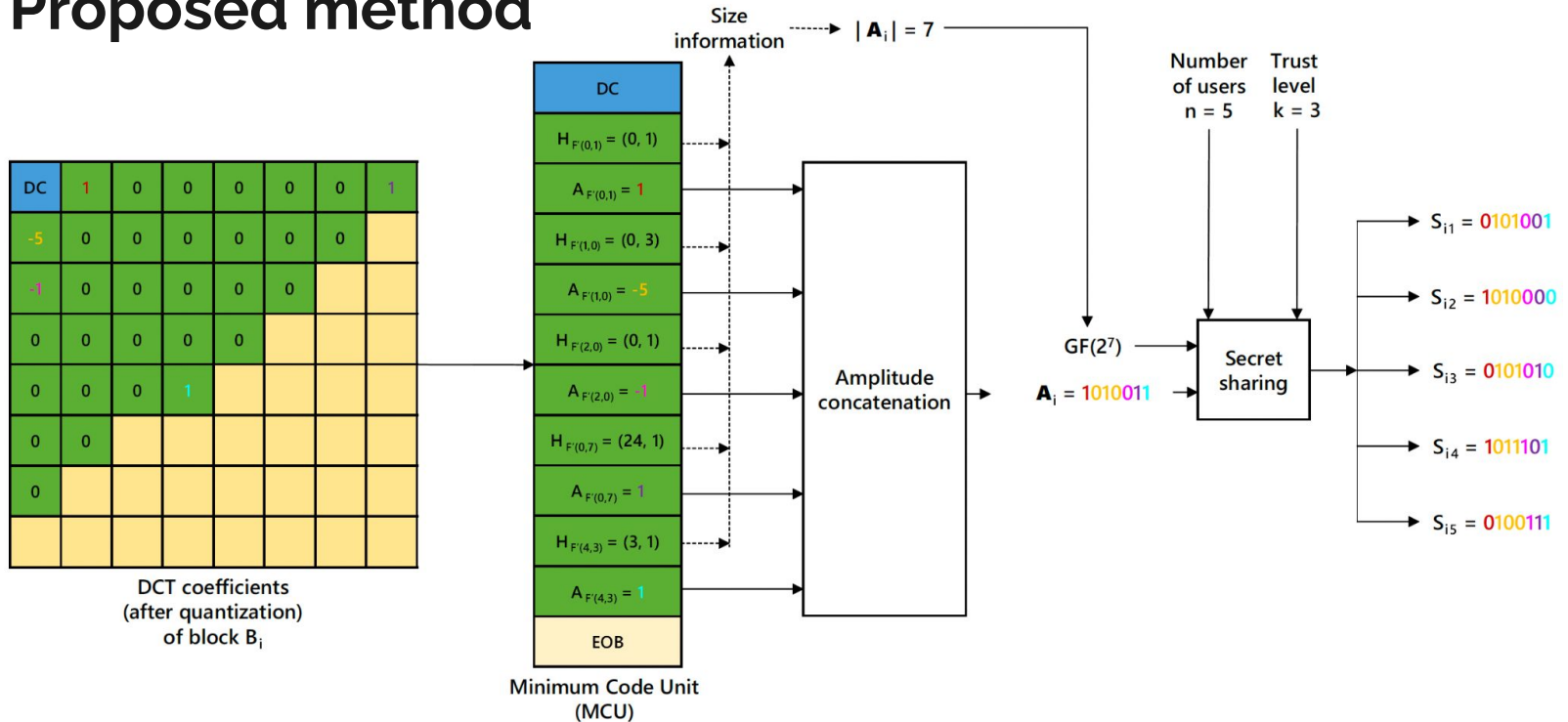




Proposed method

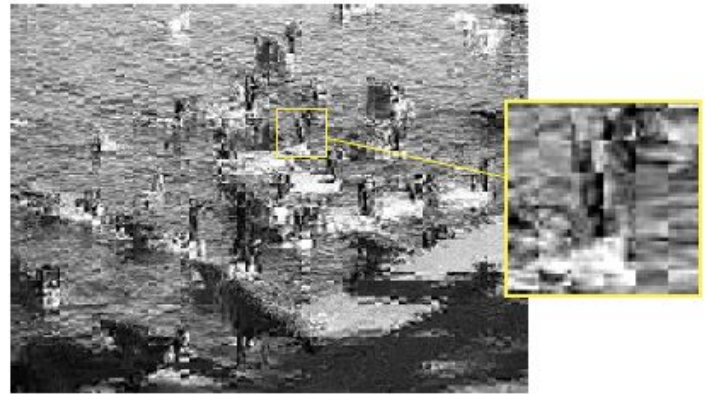
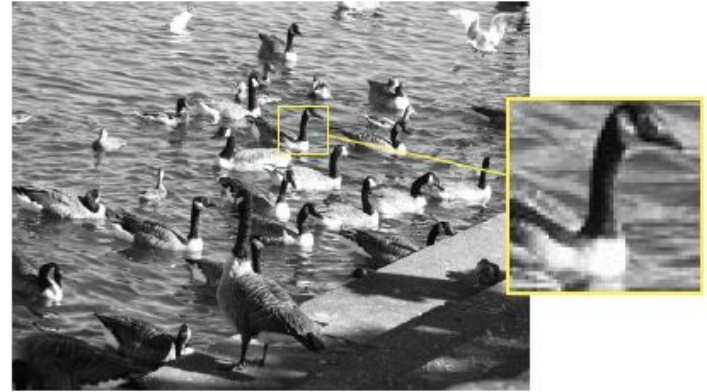
- During the **entropy coding** of JPEG
- For each quantized DCT block B_i
- **Concatenation** of the amplitudes $A_{F(u,v)}$ to obtain a **secret** A_i
 - If $|A_i| < \log_2(n+1)$: B_i remains in the clear domain.
 - If $|A_i| \geq \log_2(n+1)$:
 - **(k,n) -secret sharing over the Galois field $GF(2^{|A_i|})$**
 - n shared values S_{ij} obtained ($1 \leq j \leq n$)
 - S_{ij} injected by substitution into each shared JPEG image SI_j

Proposed method



Detailed example

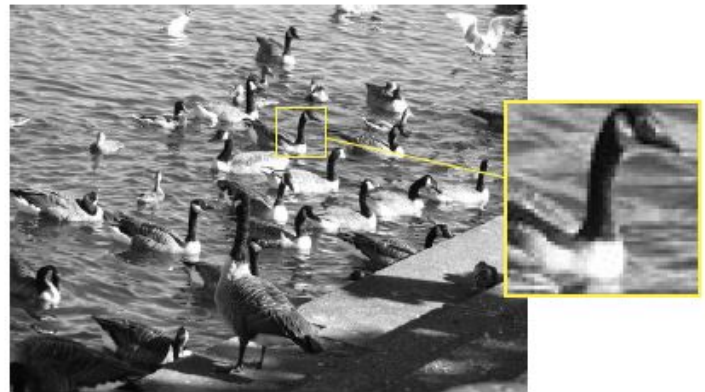
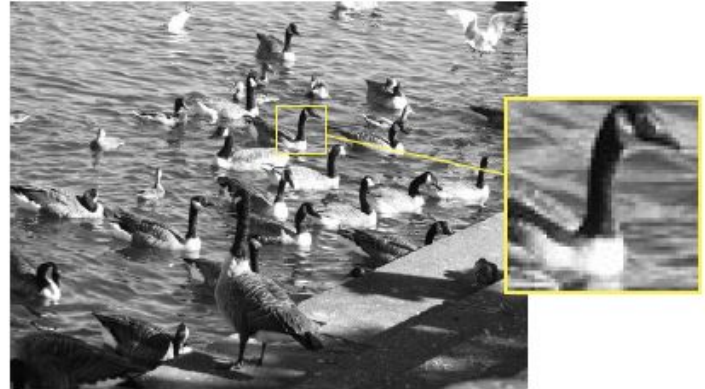
- Original uncompressed image (197 kB) from UCID database.
- Shared JPEG image, with $k = 3$, $n = 5$ and $QF = 90$ (79 kB).
- **High frequency details are secured** (PSNR = 14 dB).
- Compressed shared images are of the **same size** as the reconstructed image.



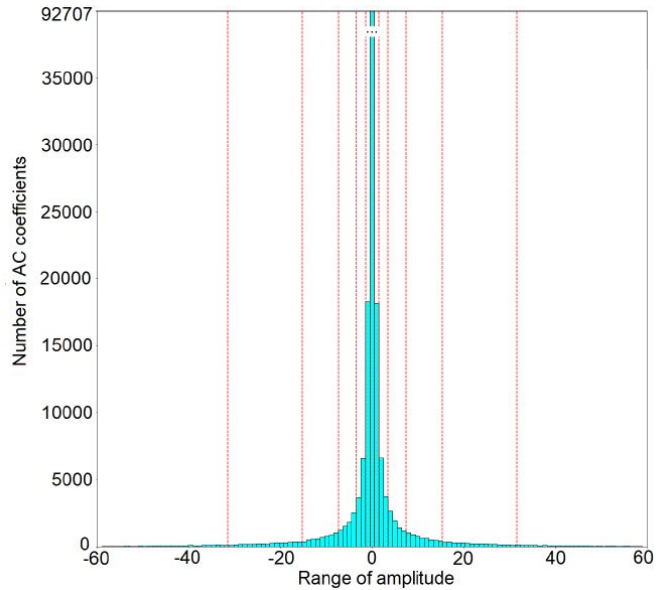
Detailed example

- Original image directly compressed with JPEG, QF = 90 (79 kB).
- Reconstructed JPEG image, QF = 90 (79 kB).

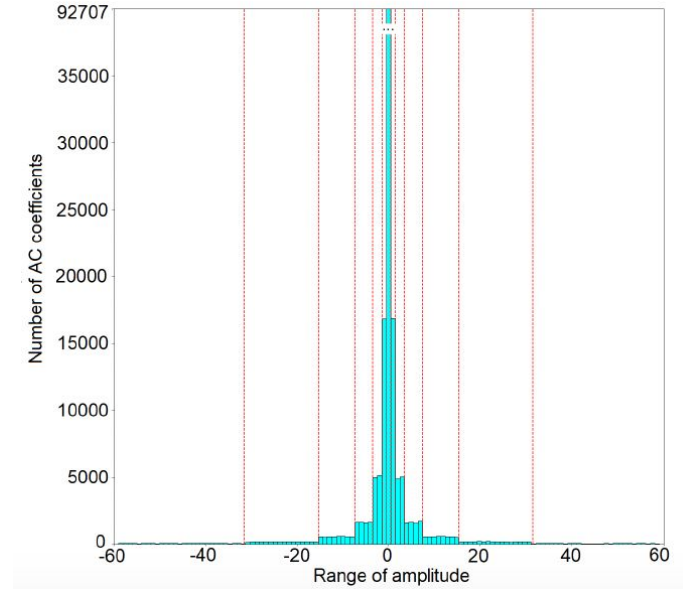
- The two images are the same.



AC coefficients' distribution



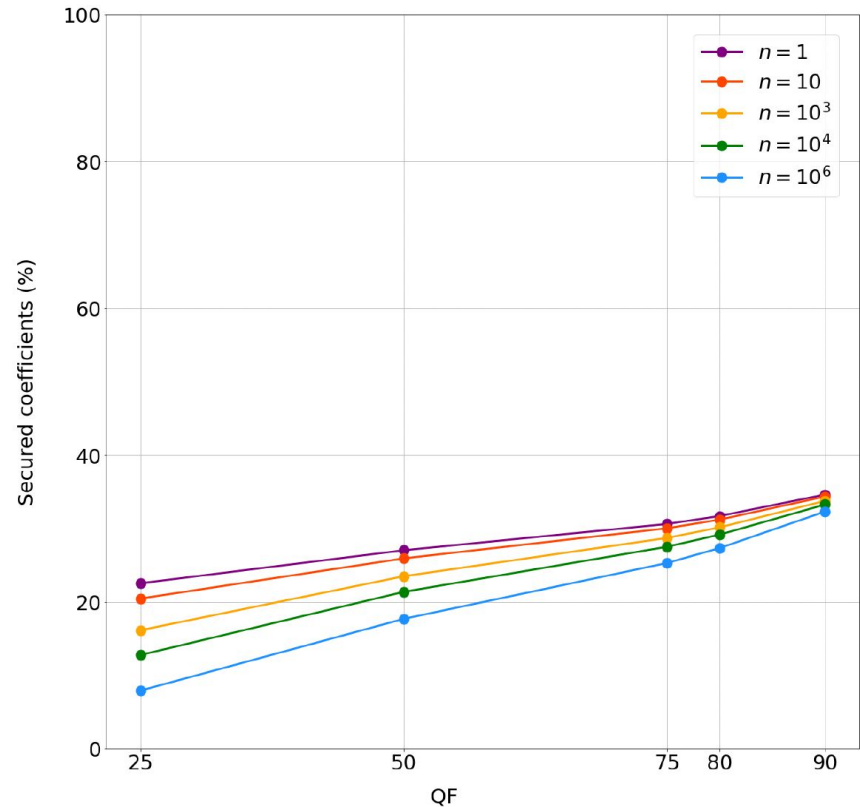
JPEG compressed image (QF = 90).



Shared JPEG image (QF = 90).

Sharing space

- Percentage of secured bits over the image size (in bits), as a function of the QF.
- The bigger is n , the larger is the number of blocks that remain in clear.
- Similar results as with JPEG crypto-compression.

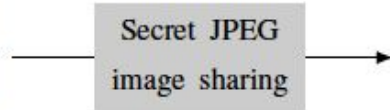


Visual security levels (color image)

- QF = 90.
- Four possible combinations of our method.



Original image



AC only



AC + DC



Luminance only

Luminance + Chrominance





Conclusion and perspectives

- Secret sharing over **Galois fields** along with JPEG compression.
- **Fully format compliant** and **size preserving** method.
- **Sufficient visual security level** (identical to crypto-compression methods).

Future work?

- Studying the impact of a noisy shared JPEG image during reconstruction.

Thank you for your attention!

Our paper: P. Puteaux, F. Yriarte, and W. Puech. "A Secret JPEG Image Sharing Method Over $GF(2^M)$ Galois Fields."
IEEE Transactions on Circuits and Systems for Video Technology, vol. 33, no. 6, pp. 3030-3042, 2023.

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