

Multi-Cloud Storage Management

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Supervised by : Gilles Seghaier

The logo for REDOCS, featuring the word "REDOCS" in a bold, sans-serif font. The "R" is orange, and the "E" is grey, while the remaining letters are black.

November 2023

The logo for s@movar, featuring the text "s@movar" in a blue, sans-serif font with a stylized '@' symbol.The logo for LIMOS, featuring the word "LIMOS" in a blue, sans-serif font with binary code (0s and 1s) integrated into the letters.The logo for DEEL, featuring the word "DEEL" in a blue, sans-serif font with a red vertical bar between the "E"s. Below it, the text "Dependable & Explainable Learning" is written in a smaller font.

INSTITUT
POLYTECHNIQUE
DE PARIS

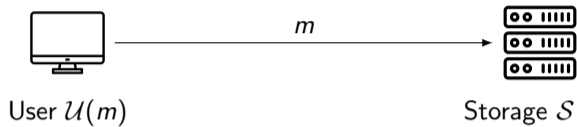
The logo for UCA, featuring the letters "UCA" in a blue, sans-serif font above the text "UNIVERSITÉ Clermont Auvergne" in a smaller font.The logo for UQAM, featuring the text "UQAM" in a blue, sans-serif font with a stylized 'A'.

Astran

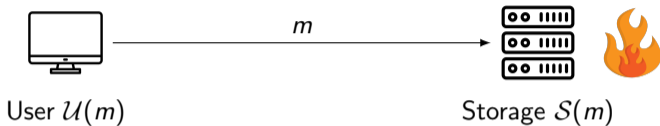


- Sensitive data storage
- Availability
- 20 employees
- 4.5 M€

Problematic of the Single-storage



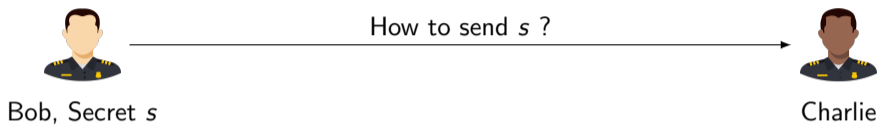
Problematic of the Single-storage



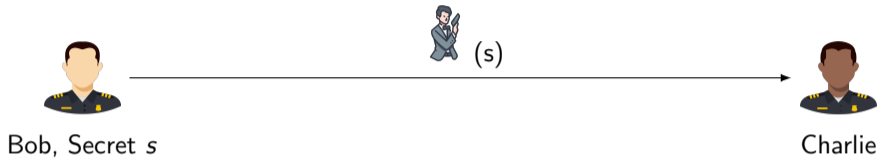
Can we do better ? YES

- With redundancy, but not fun !
- With **secret sharing**

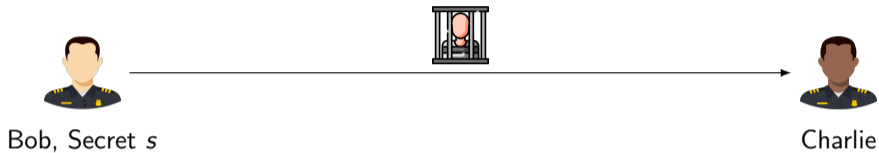
Secret-Sharing (SS)



Secret-Sharing (SS)



Secret-Sharing (SS)



Secret leaked if spy is captured !

Secret-Sharing (SS)

$$s = s_1 || \dots || s_5$$



Bob, Secret s

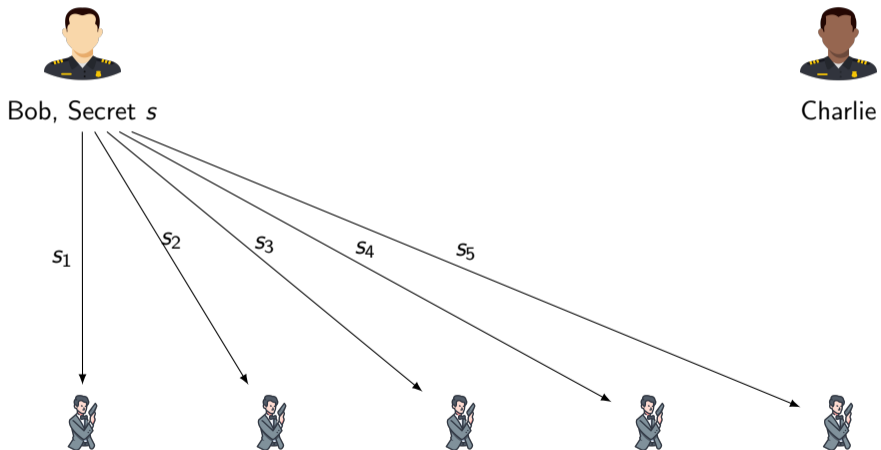


Charlie



Secret-Sharing (SS)

$$s = s_1 || \dots || s_5$$



Secret-Sharing (SS)

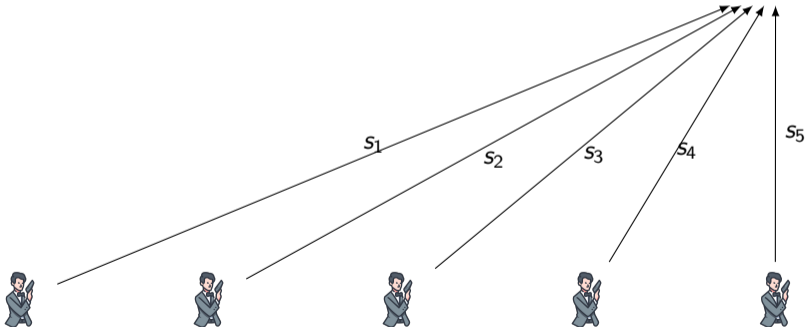
$$s = s_1 || \dots || s_5$$



Bob, Secret s



Charlie



Secret-Sharing (SS)

$$s = s_1 || \dots || s_5$$

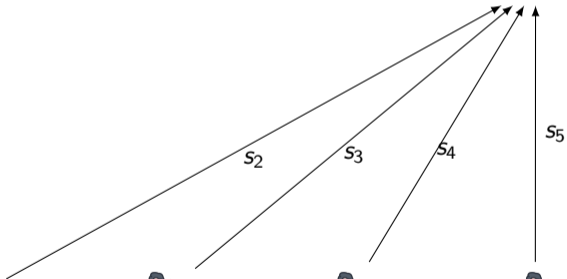


Bob, Secret s

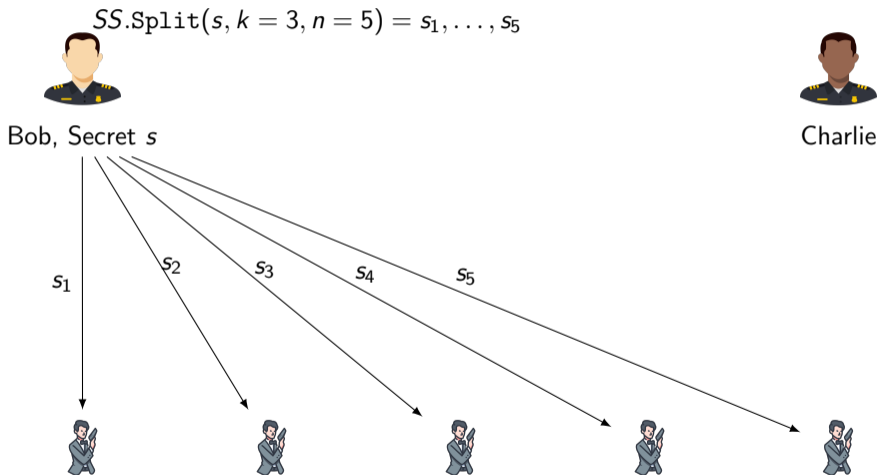
Secret lost if a spy is killed !



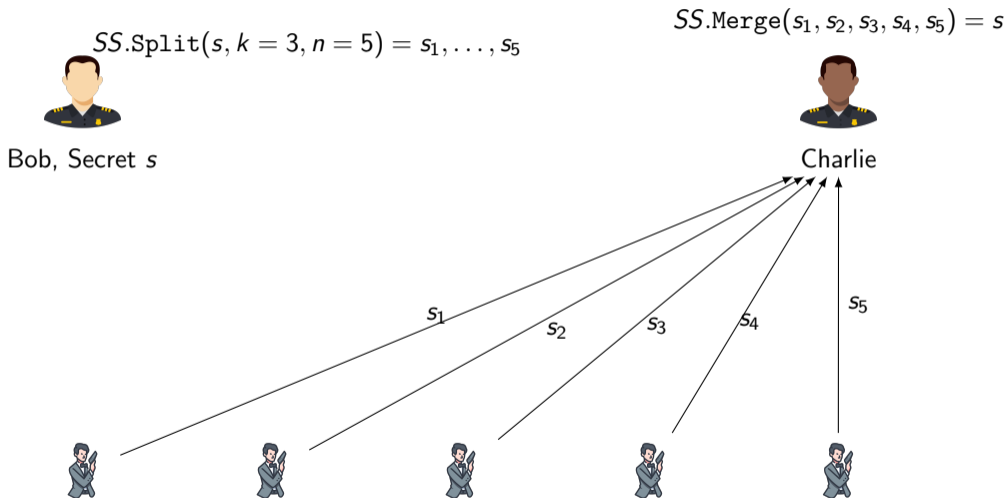
Charlie



Secret-Sharing (SS)



Secret-Sharing (SS)



Secret-Sharing (SS)

$$SS.Split(s, k = 3, n = 5) = s_1, \dots, s_5$$

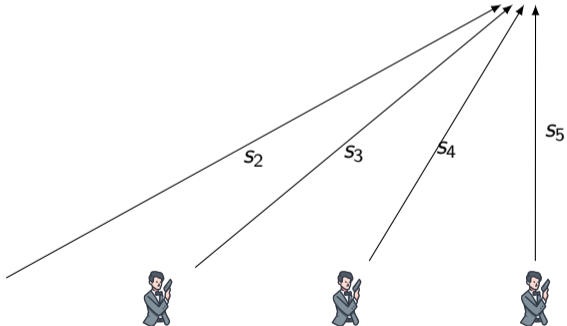


Bob, Secret s

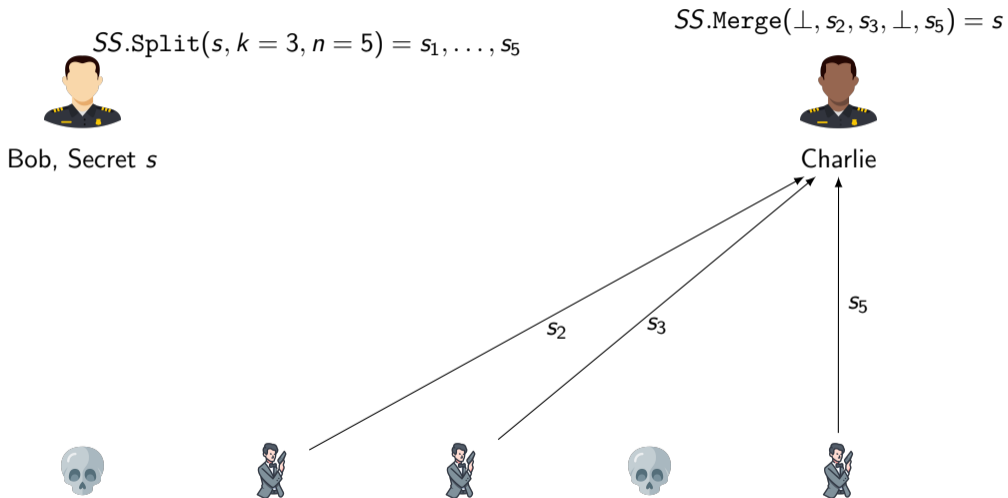
$$SS.Merge(\perp, s_2, s_3, s_4, s_5) = s$$



Charlie



Secret-Sharing (SS)



Secret-Sharing (SS)

$$SS.Split(s, k = 3, n = 5) = s_1, \dots, s_5$$



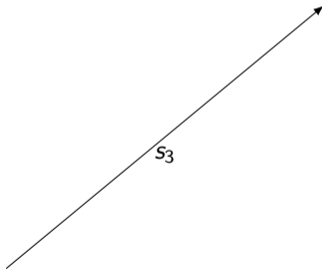
Bob, Secret s

Number of shares upper than $k - 1 \implies$ Preserved secret!

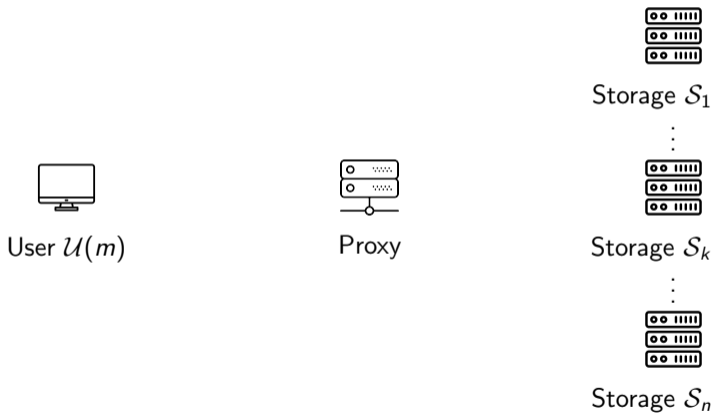
$$SS.Merge(\perp, \perp, s_3, \perp, s_5) = \perp$$



Charlie

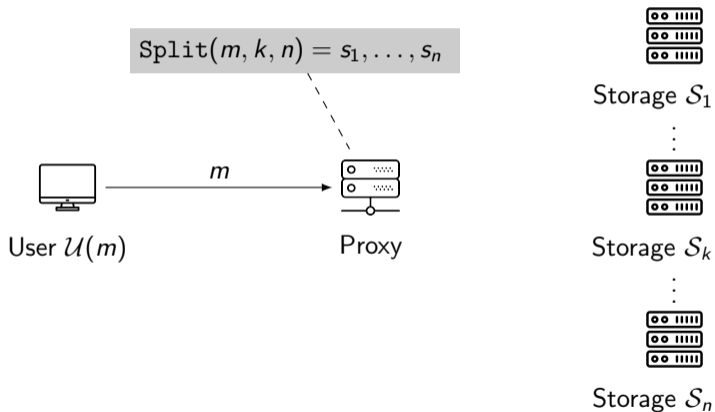


What's the problem ?



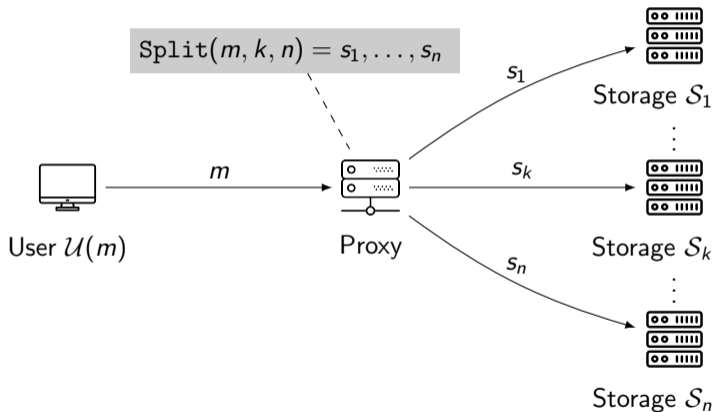
What's the problem ?

Upload



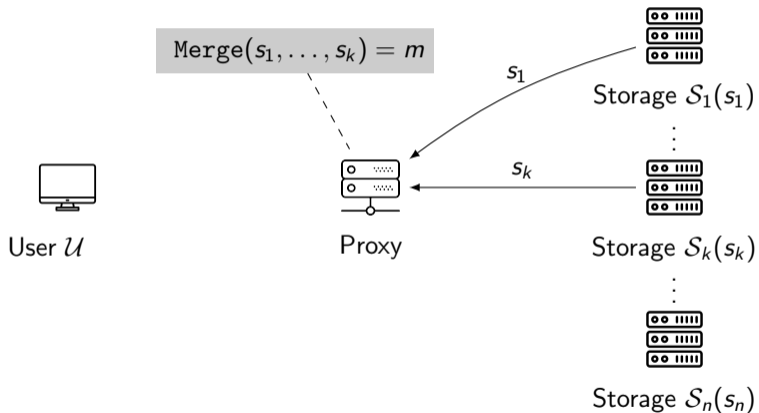
What's the problem ?

Upload



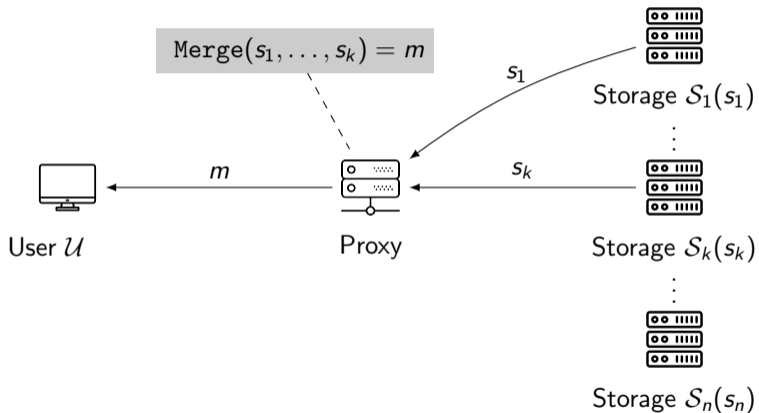
What's the problem ?

Download

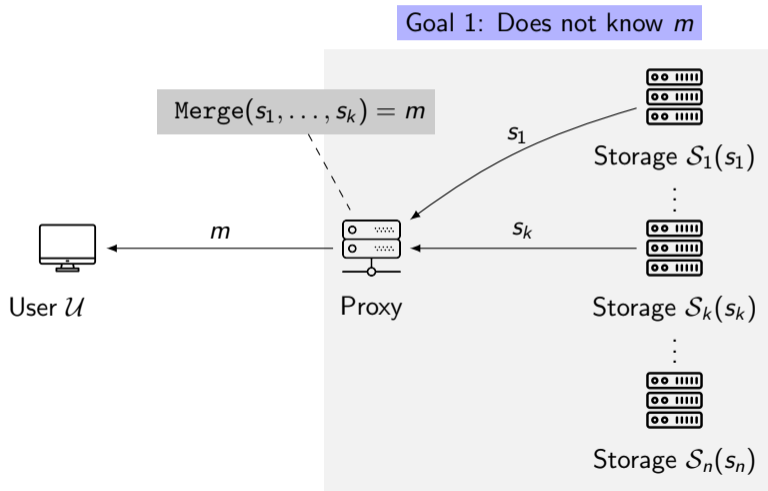


What's the problem ?

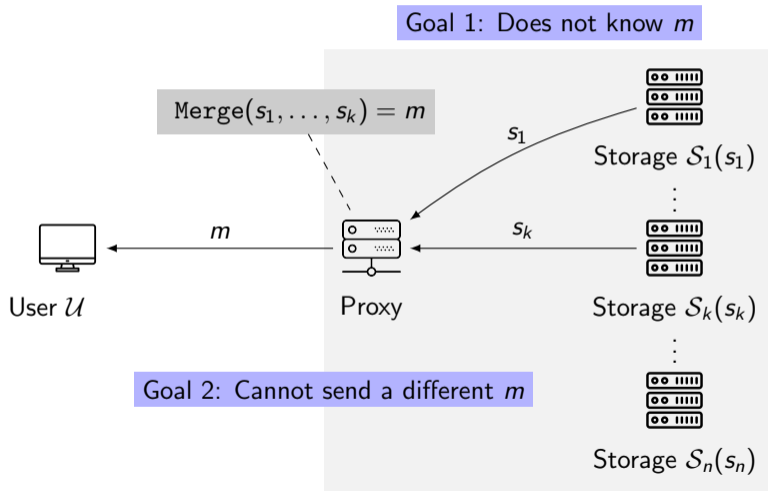
Download



What's the problem ?



What's the problem ?



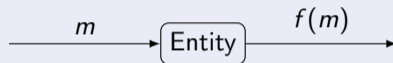
Looking for security, but against what ?



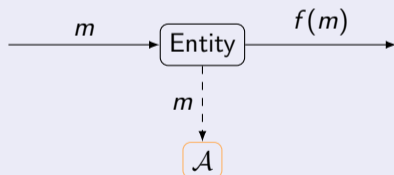
What the adversary (denoted \mathcal{A}) is able to corrupt ?

Type of adversary \mathcal{A}

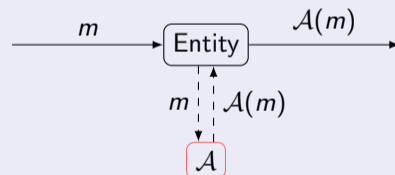
Honest



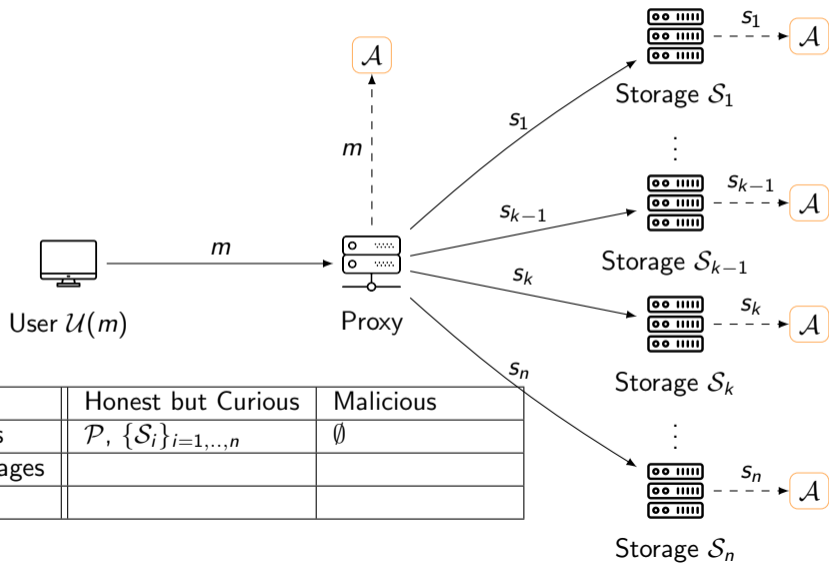
Honest-but-Curious



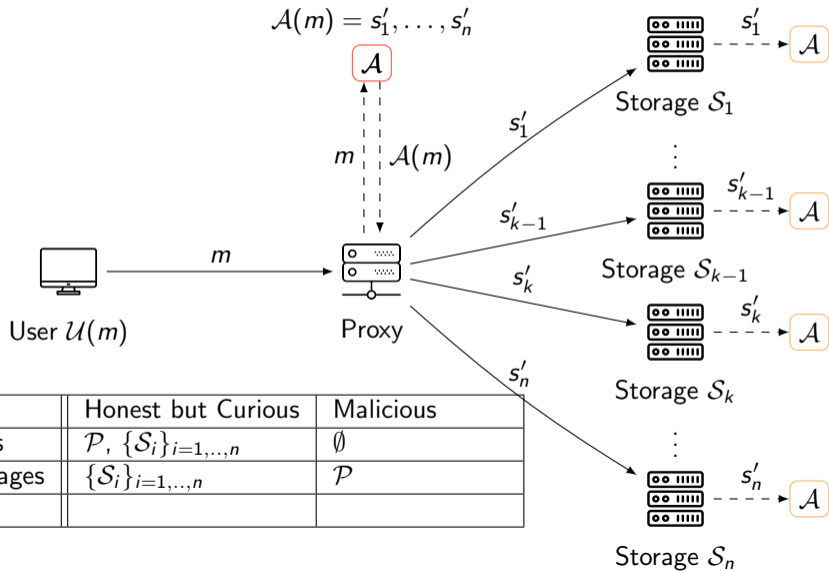
Malicious



Corruption Model

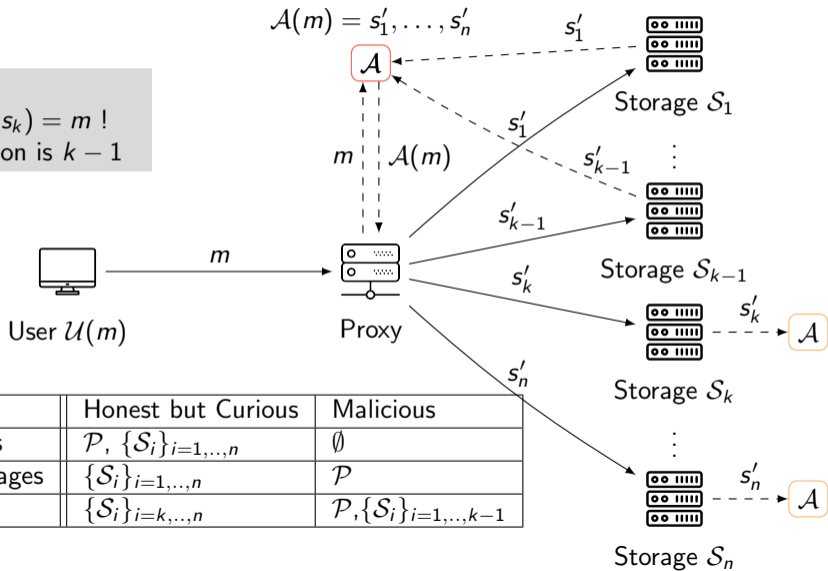


Corruption Model



Corruption Model

Recall that
 $\text{Merge}(s_1, \dots, s_k) = m$!
 So max collusion is $k - 1$



Corr. Model	Honest but Curious	Malicious
Fully-Curious	$\mathcal{P}, \{\mathcal{S}_i\}_{i=1, \dots, n}$	\emptyset
Curious Storages	$\{\mathcal{S}_i\}_{i=1, \dots, n}$	\mathcal{P}
Collusion	$\{\mathcal{S}_i\}_{i=k, \dots, n}$	$\mathcal{P}, \{\mathcal{S}_i\}_{i=1, \dots, k-1}$

Contributions

- 1 Attack against secrecy

Contributions

- 1 Attack against secrecy
- 1 Attack against confidentiality

Contributions

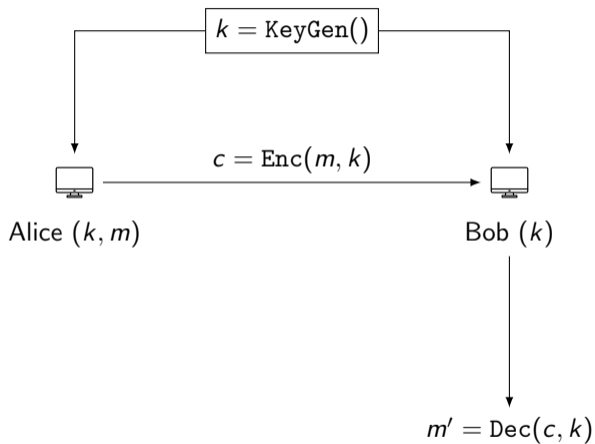
- 1 Attack against secrecy
- 1 Attack against confidentiality
- 3 new protocols

PRZT: The initial (flawed) protocol

scheme	#Users	Proxy model	#Collusions	Secrecy	Integrity
<i>PRZT</i>	1	Honest but Curious	0	✓	✓

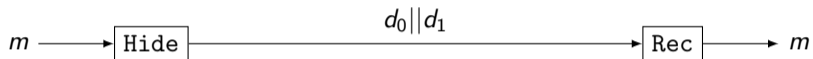
Primitive	Introduced	Algorithms
Secret Sharing	✓	Split, Merge
Proxy Homomorphic Re-Encryption		KeyGen, Enc, Dec, ReEnc
AONT		Hide, Rec

Symmetric encryption



AONT

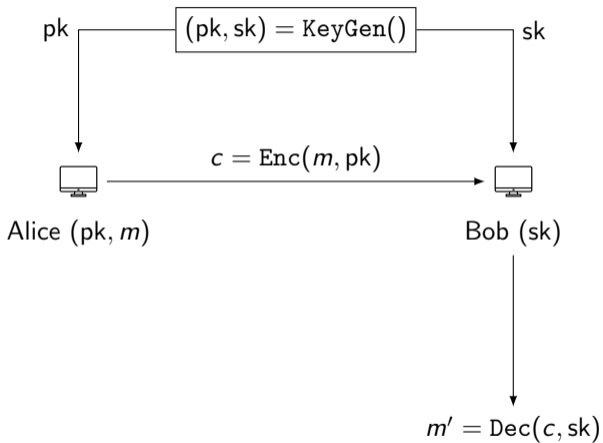
All-or-Nothing



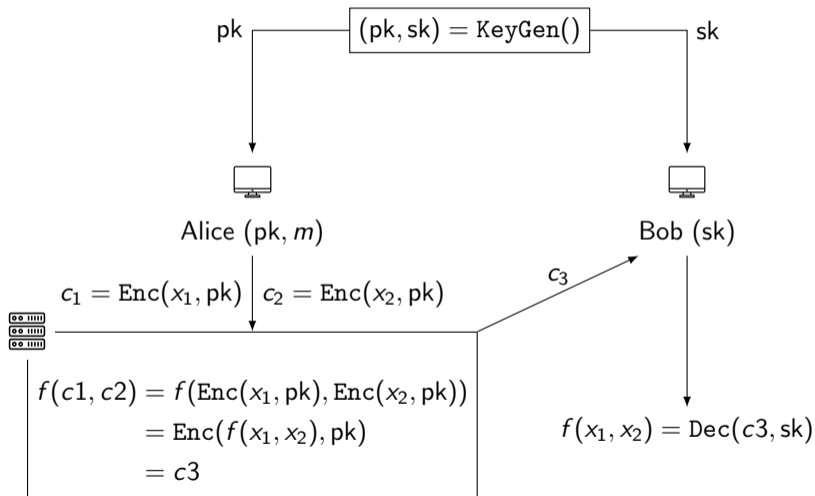
- 1 $k \leftarrow \text{Sym.KeyGen}()$
- 2 $c \leftarrow \text{Sym.Enc}(k, m || 0^\lambda)$
- 3 $d_0 \leftarrow c$
- 4 $d_1 \leftarrow k \oplus H(c)$

- 1 $k \leftarrow d_1 \oplus H(d_0)$
- 2 $m' \leftarrow \text{Sym.Dec}(k, d_0)$
- 3 Check that $m' = m || 0^\lambda$

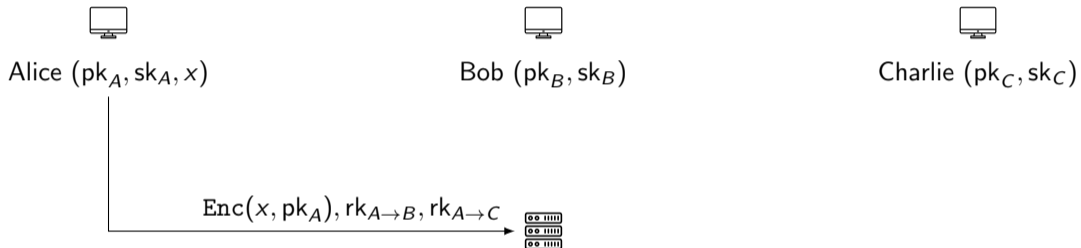
Public Key Encryption (PKE)



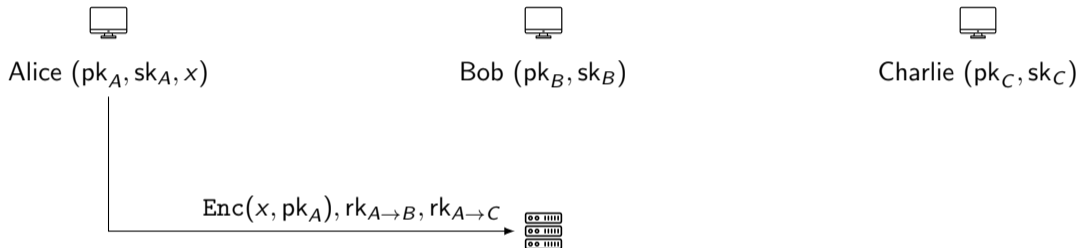
Public Key Homomorphic Encryption



Proxy Homomorphic Re-Encryption (PRE)



Proxy Homomorphic Re-Encryption (PRE)

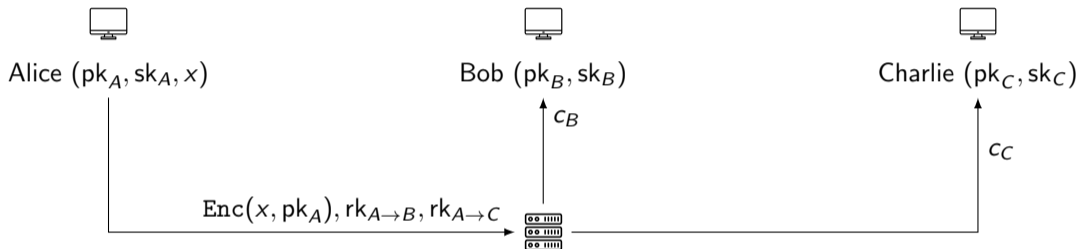


$$1 \quad f(\text{Enc}(x, pk_A)) = \text{Enc}(f(x), pk_A) = c_A$$

$$2 \quad \text{ReEnc}(c_A, rk_{A \rightarrow B}) = \text{Enc}(f(x), pk_B) = c_B$$

$$3 \quad \text{ReEnc}(c_A, rk_{A \rightarrow C}) = \text{Enc}(f(x), pk_C) = c_C$$

Proxy Homomorphic Re-Encryption (PRE)



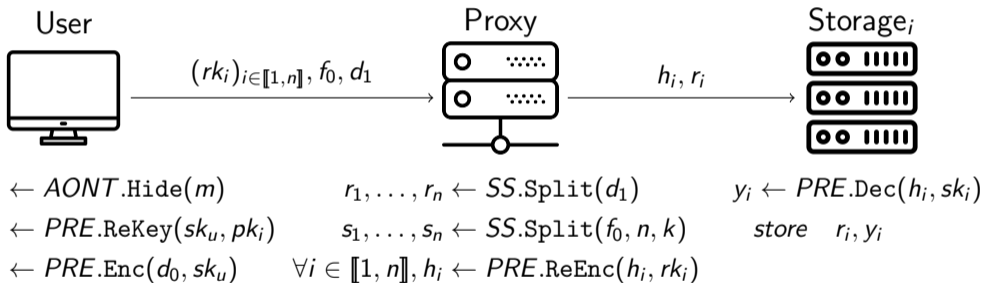
$$1 \quad f(Enc(x, pk_A)) = Enc(f(x), pk_A) = c_A$$

$$2 \quad ReEnc(c_A, rk_{A \rightarrow B}) = Enc(f(x), pk_B) = c_B$$

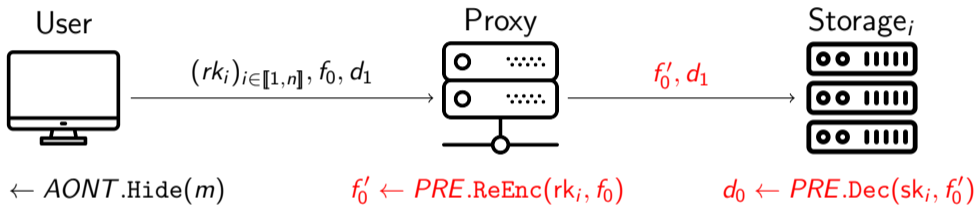
$$3 \quad ReEnc(c_A, rk_{A \rightarrow C}) = Enc(f(x), pk_C) = c_C$$

PRZT: The initial (flawed) protocol

Upload only



PRZT: A Forward-Attack



$$d_0 || d_1 \leftarrow AONT.Hide(m)$$

$$\forall i \in \llbracket 1, n \rrbracket, rk_i \leftarrow PRE.ReEnc(sk_u, pk_i)$$

$$f_0 \leftarrow PRE.Enc(d_0, sk_u)$$

$$f'_0 \leftarrow PRE.ReEnc(rk_i, f_0)$$

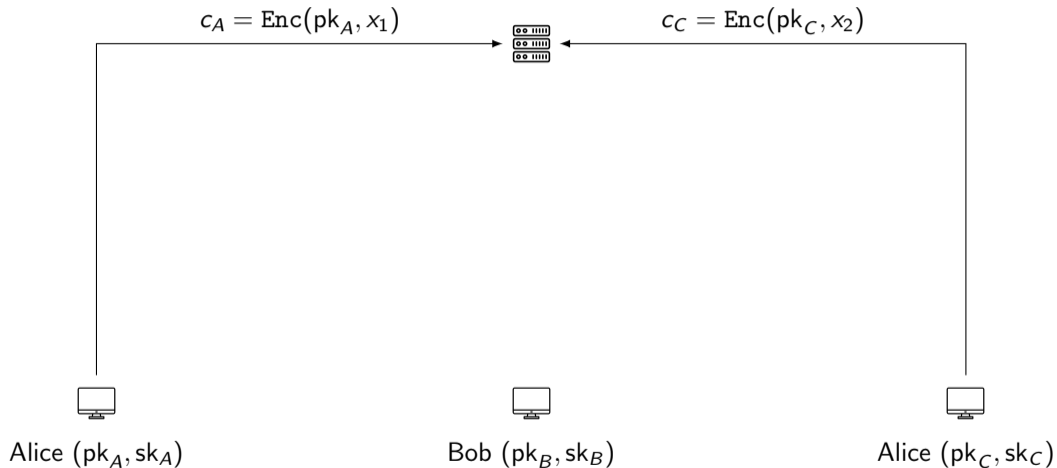
$$d_0 \leftarrow PRE.Dec(sk_i, f'_0)$$

MKZT: Multi-Key Homomorphic Encryption-based Protocol

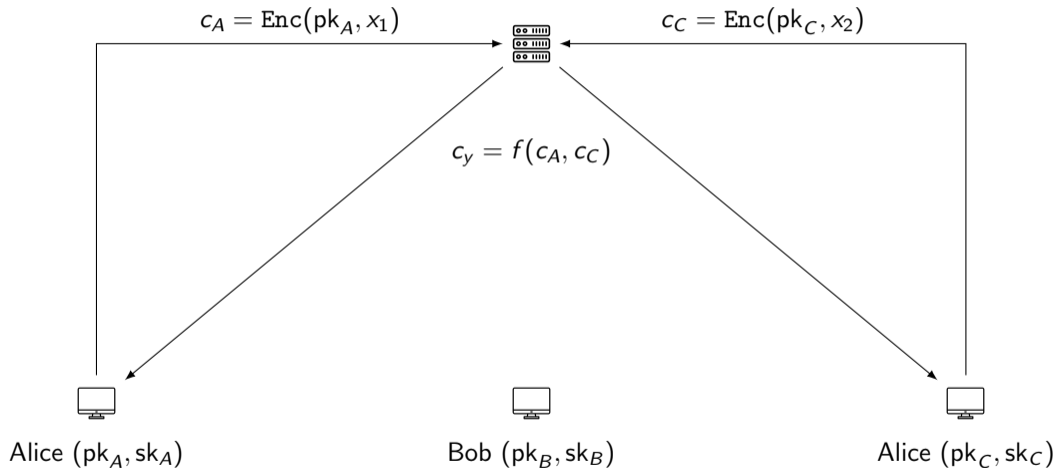
scheme	#Users	Proxy	#Collusions	Secrecy	Integrity
<i>PRZT</i>	1	Honest but Curious	✓	✓	✓
<i>MKZT</i>	1	Honest but Curious	✓	✓	✓

Primitive	Introduced	Algorithms
Secret Sharing (SS)	✓	Split, Merge
Multi-key Homomorphic Encryption (MKE)		KeyGen, Enc, PartDec, FinDec
AONT	✓	Hide, Rec

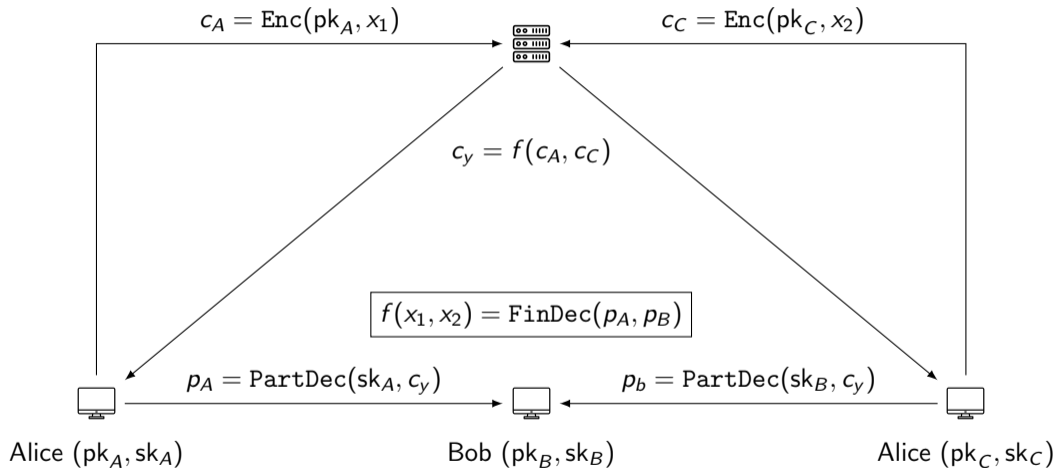
Multi-Key Homomorphic Encryption (MKE)



Multi-Key Homomorphic Encryption (MKE)

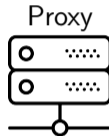


Multi-Key Homomorphic Encryption (MKE)



MKZT

Upload

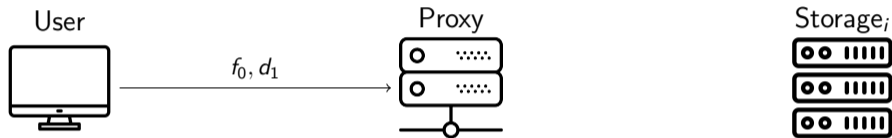


$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$f_0 \leftarrow \text{MKE.Enc}((pk_i)_{i \in [1, n]}, d_0)$$

MKZT

Upload

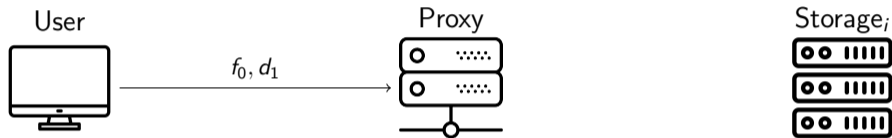


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MKZT

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

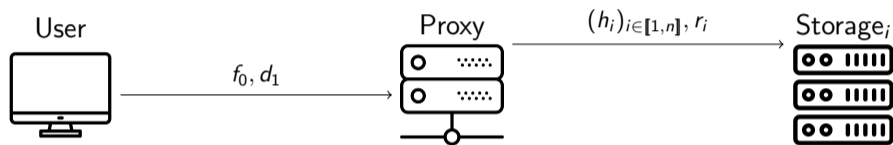
$$f_0 \leftarrow \text{MKE.Enc}((pk_i)_{i \in [1, n]}, d_0)$$

$$h_1, \dots, h_n \leftarrow \text{SS.Split}(f_0)$$

$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

MKZT

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

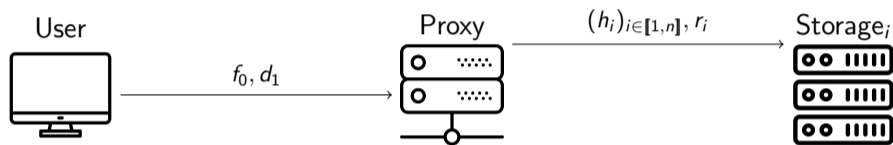
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MKZT

Upload



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$$h_1, \dots, h_n \leftarrow \text{SS.Split}(f_0)$$

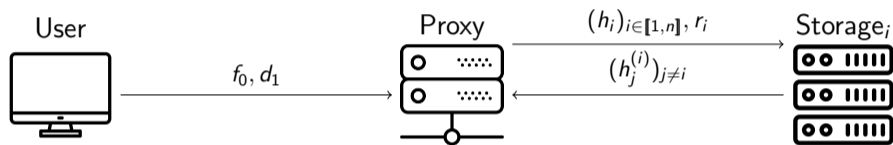
$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

$$\forall j \in [1, n],$$

$$h_j^{(i)} \leftarrow \text{MKE.PartDec}(sk_i, h_j)$$

MKZT

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$f_0 \leftarrow \text{MKE.Enc}((pk_i)_{i \in [1, n]}, d_0)$$

$$h_1, \dots, h_n \leftarrow \text{SS.Split}(f_0)$$

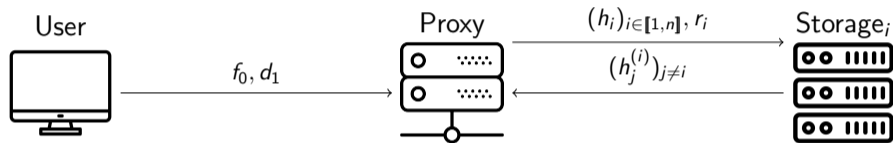
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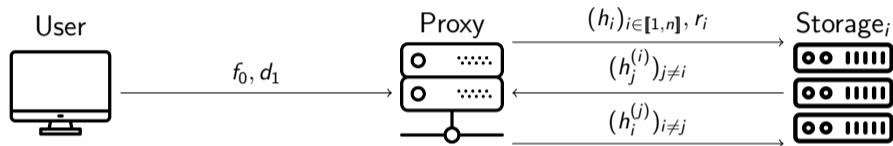
$$h_j^{(i)} \leftarrow \text{MKE.PartDec}(sk_i, h_j)$$

$$y_i \leftarrow \text{MKE.FinDec}((h_j^{(i)})_{j \in [1, n]})$$

store r_i, y_i

MKZT

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$f_0 \leftarrow \text{MKE.Enc}((pk_i)_{i \in [1, n]}, d_0)$$

$$h_1, \dots, h_n \leftarrow \text{SS.Split}(f_0)$$

$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

$$\forall j \in [1, n],$$

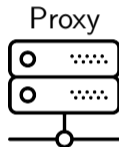
$$h_j^{(i)} \leftarrow \text{MKE.PartDec}(sk_i, h_j)$$

$$y_i \leftarrow \text{MKE.FinDec}((h_i^{(j)})_{j \in [1, n]})$$

$$\textit{store } r_i, y_i$$

MKZT

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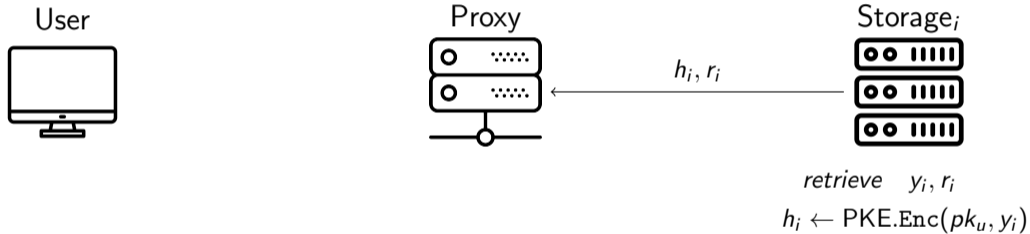


retrieve y_i, r_i

$h_j \leftarrow \text{PKE.Enc}(pk_u, y_i)$

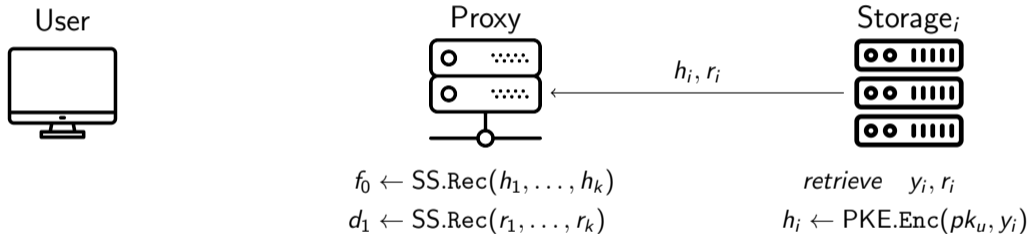
MKZT

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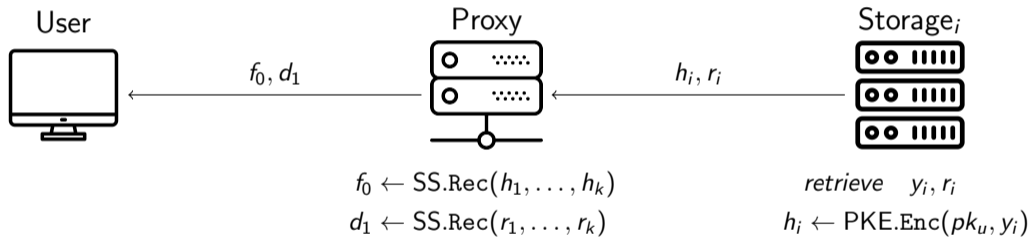
MKZT

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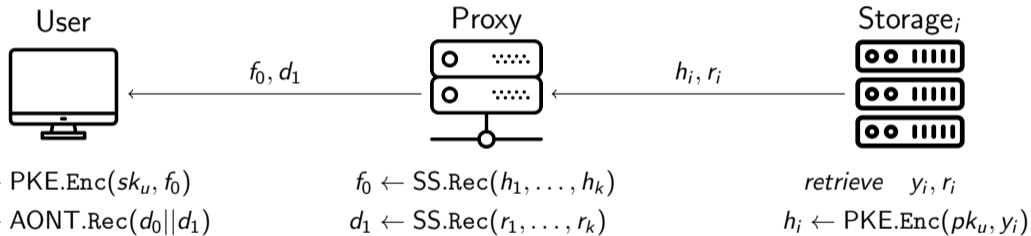
MKZT

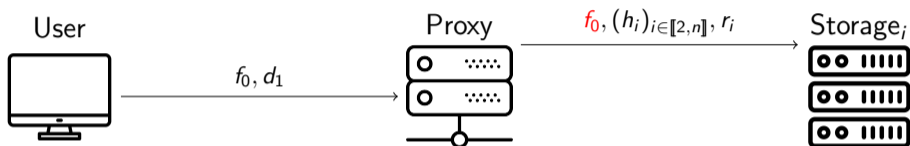
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MKZT

download



MKZT is under attack

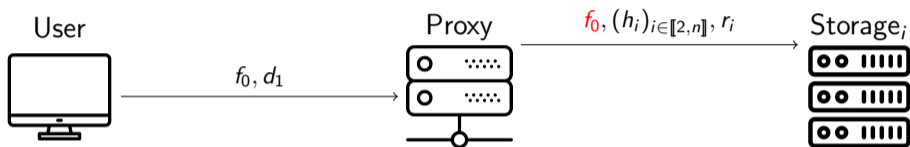
$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$f_0 \leftarrow \text{MKE.Enc}((pk_i)_{i \in [1, n]}, d_0)$$

$$h_1, \dots, h_n \leftarrow \text{SS.Split}(f_0)$$

$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

$$f_0^{(0)} \leftarrow \text{MKE.PartDec}(sk_0, f_0)$$

MKZT is under attack

$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

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$$h_1, \dots, h_n \leftarrow \text{SS.Split}(f_0)$$

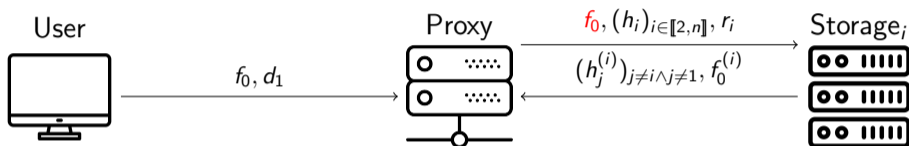
$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

$$f_0^{(0)} \leftarrow \text{MKE.PartDec}(sk_0, f_0)$$

$$\forall j \in [2, n],$$

$$h_j^{(i)} \leftarrow \text{MKE.PartDec}(sk_i, h_j)$$

$$f_0^{(i)} \leftarrow \text{MKE.PartDec}(sk_i, f_0)$$

MKZT is under attack

$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$f_0 \leftarrow \text{MKE.Enc}((pk_i)_{i \in [1, n]}, d_0)$$

$$h_1, \dots, h_n \leftarrow \text{SS.Split}(f_0)$$

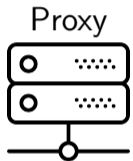
$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

$$f_0^{(0)} \leftarrow \text{MKE.PartDec}(sk_0, f_0)$$

$$d_0 \leftarrow \text{MKE.FinDec}((f_0^{(j)})_{j \in [1, n]})$$

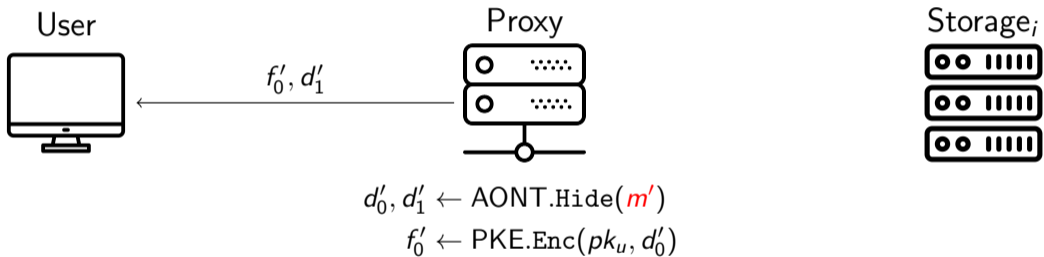
$$m \leftarrow \text{AONT.Rec}(d_0 || d_1)$$

MKZT is under attack again

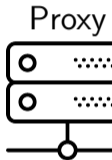


$$d'_0, d'_1 \leftarrow \text{AONT.Hide}(m')$$

$$f'_0 \leftarrow \text{PKE.Enc}(pk_u, d'_0)$$

MKZT is under attack again

MKZT is under attack again


 f'_0, d'_1


$$d'_0 \leftarrow \text{PKE.Enc}(sk_u, f'_0)$$

$$m' \leftarrow \text{AONT.Rec}(d'_0 || d'_1)$$

$$d'_0, d'_1 \leftarrow \text{AONT.Hide}(m')$$

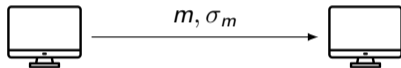
$$f'_0 \leftarrow \text{PKE.Enc}(pk_u, d'_0)$$

PRZT+: (Improved) Proxy Re-Encryption-based Protocol

scheme	#Users	Proxy model	#Collusions	Secrecy	Integrity
<i>PRZT</i>	1	Honest but Curious	0	✓	✓
<i>MKZT</i>	1	Honest but Curious	k-1	✓	✓
<i>PRZT+</i>	1	Malicious	k-1	✓	✓

Primitive	Introduced	Algorithms
Secret Sharing (SS)	✓	Split, Merge
Public Key Encryption (PKE)	✓	KeyGen, Enc, Dec
Signature (Sig)		KeyGen, Sign, Verif
AONT	✓	Hide, Rec

Signature

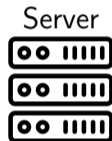
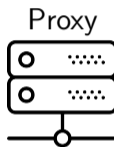


$$\sigma_m \leftarrow \text{Sign}(\text{sk}, m)$$

$$\top/\perp \leftarrow \text{Verif}(\text{pk}, m, \sigma_m)$$

PRZT+

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

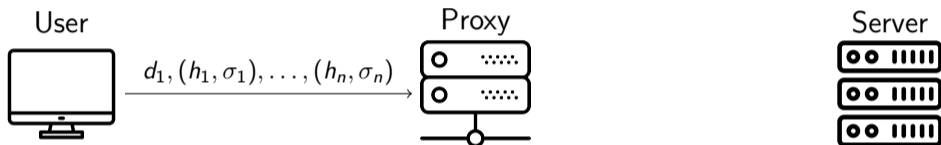
$$s_1, \dots, s_n \leftarrow \text{SS.Split}(d_0, n, k)$$

$$h_i \leftarrow \text{PKE.Enc}(pk_i, s_i)$$

$$\sigma_i \leftarrow \text{Sig.Sign}(sk_u, h_i)$$

PRZT+

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

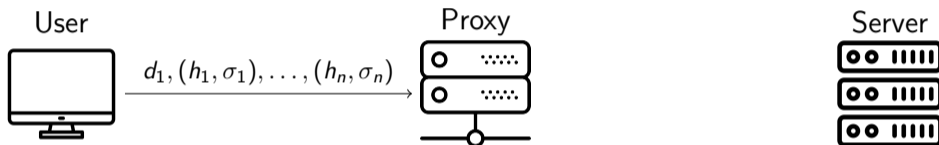
$$s_1, \dots, s_n \leftarrow \text{SS.Split}(d_0, n, k)$$

$$h_i \leftarrow \text{PKE.Enc}(pk_i, s_i)$$

$$\sigma_i \leftarrow \text{Sig.Sign}(sk_u, h_i)$$

PRZT+

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$s_1, \dots, s_n \leftarrow \text{SS.Split}(d_0, n, k)$$

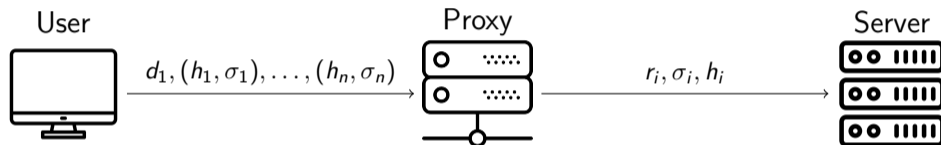
$$h_i \leftarrow \text{PKE.Enc}(pk_i, s_i)$$

$$\sigma_i \leftarrow \text{Sig.Sign}(sk_u, h_i)$$

$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

PRZT+

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$s_1, \dots, s_n \leftarrow \text{SS.Split}(d_0, n, k)$$

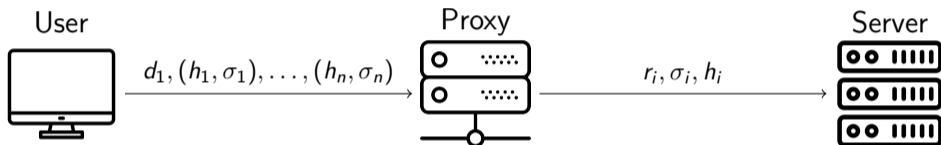
$$h_i \leftarrow \text{PKE.Enc}(pk_i, s_i)$$

$$\sigma_i \leftarrow \text{Sig.Sign}(sk_u, h_i)$$

$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

PRZT+

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$s_1, \dots, s_n \leftarrow \text{SS.Split}(d_0, n, k)$$

$$h_i \leftarrow \text{PKE.Enc}(pk_i, s_i)$$

$$\sigma_i \leftarrow \text{Sig.Sign}(sk_u, h_i)$$

$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

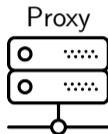
$$\text{Sig.Verif}(pk_u, \sigma_i, h_i,)$$

$$y_i \leftarrow \text{PKE.Dec}(sk_i, h_i)$$

$$\text{store } r_i, y_i$$

PRZT+

Download

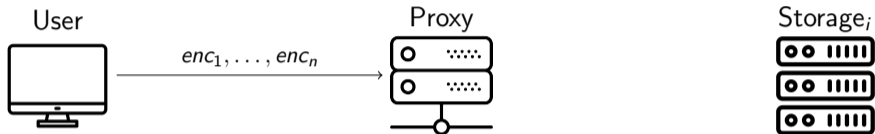


$$nc_1, \dots, nc_n \leftarrow \text{PKE.Gen}(\lambda)$$

$$\forall i \in \llbracket 1, n \rrbracket, enc_i \leftarrow \text{PKE.Enc}(pk_i, nc_i)$$

PRZT+

Download

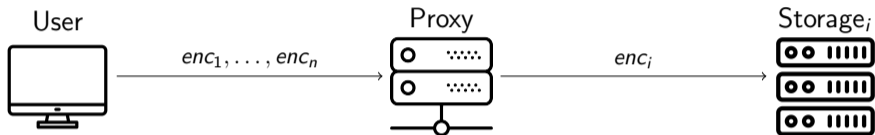


$$nc_1, \dots, nc_n \leftarrow \text{PKE.Gen}(\lambda)$$

$$\forall i \in \llbracket 1, n \rrbracket, enc_i \leftarrow \text{PKE.Enc}(pk_i, nc_i)$$

PRZT+

Download

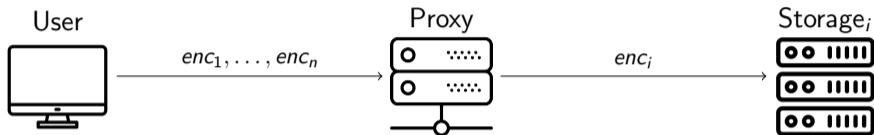


$$nc_1, \dots, nc_n \leftarrow \text{PKE.Gen}(\lambda)$$

$$\forall i \in \llbracket 1, n \rrbracket, enc_i \leftarrow \text{PKE.Enc}(pk_i, nc_i)$$

PRZT+

Download



$$nc_1, \dots, nc_n \leftarrow \text{PKE.Gen}(\lambda)$$

$$\forall i \in \llbracket 1, n \rrbracket, enc_i \leftarrow \text{PKE.Enc}(pk_i, nc_i)$$

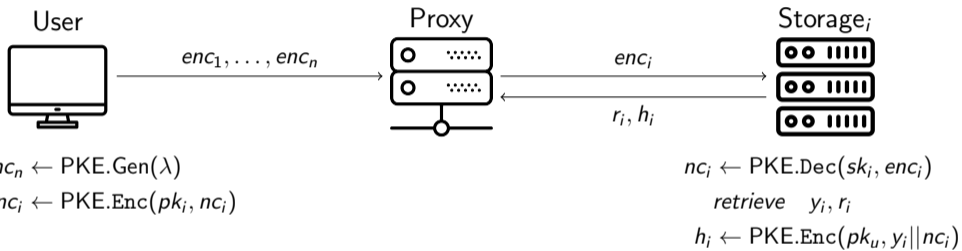
$$nc_i \leftarrow \text{PKE.Dec}(sk_i, enc_i)$$

retrieve y_i, r_i

$$h_i \leftarrow \text{PKE.Enc}(pk_u, y_i || nc_i)$$

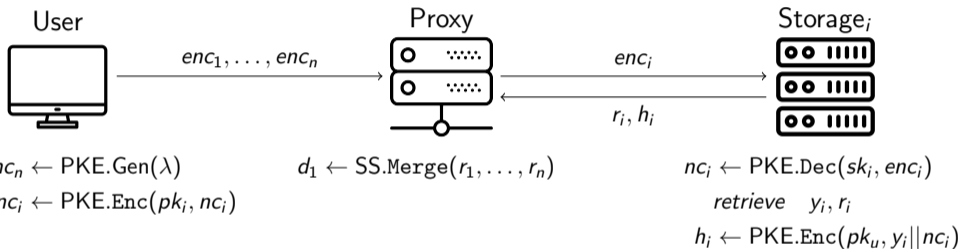
PRZT+

Download



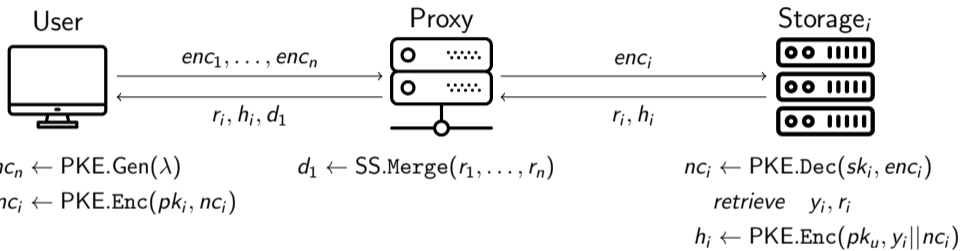
PRZT+

Download



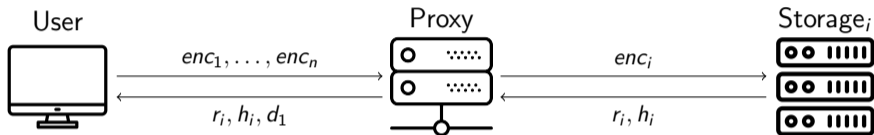
PRZT+

Download



PRZT+

Download



$$nc_1, \dots, nc_n \leftarrow \text{PKE.Gen}(\lambda)$$

$$\forall i \in \llbracket 1, n \rrbracket, enc_i \leftarrow \text{PKE.Enc}(pk_i, nc_i)$$

$$\forall i \in \llbracket 1, n \rrbracket, y_i || nc_i \leftarrow \text{PKE.Dec}(sk_u, h_i)$$

$$\text{verify } (nc_i)_{i \in I}, I \subset \llbracket 1, n \rrbracket \wedge |I| = k$$

$$d_0 \leftarrow \text{SS.Merge}(y_1, \dots, y_k)$$

$$m \leftarrow \text{AONT.Rec}(d_0 || d_1)$$

$$d_1 \leftarrow \text{SS.Merge}(r_1, \dots, r_n)$$

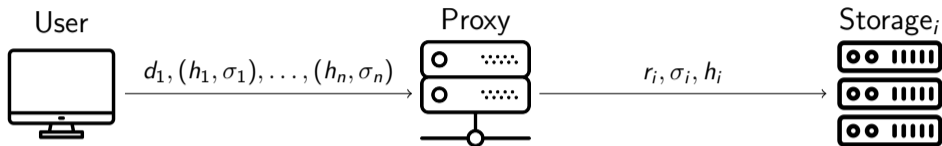
$$nc_i \leftarrow \text{PKE.Dec}(sk_i, enc_i)$$

$$\text{retrieve } y_i, r_i$$

$$h_i \leftarrow \text{PKE.Enc}(pk_u, y_i || nc_i)$$

PRZT+

Pros and cons



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$s_1, \dots, s_n \leftarrow \text{SS.Split}(d_0, n, k)$$

$$h_i \leftarrow \text{PKE.Enc}(pk_i, s_i)$$

$$\sigma_i \leftarrow \text{Sig.Sign}(sk_u, h_i)$$

$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

$$\text{Sig.Verif}(pk_u, \sigma_i, h_i,)$$

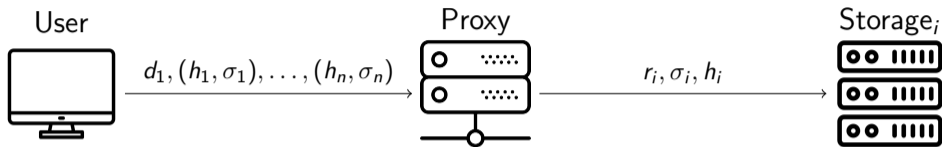
$$y_i \leftarrow \text{PKE.Dec}(sk_i, h_i)$$

store r_i, y_i

	#Users	Proxy model	#Collusions	Secrecy	Integrity	Authentication authority
<i>PRZT+</i>	1	Malicious	k-1	✓	✓	✓

PRZT+

Pros and cons



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$s_1, \dots, s_n \leftarrow \text{SS.Split}(d_0, n, k)$$

$$h_i \leftarrow \text{PKE.Enc}(pk_i, s_i)$$

$$\sigma_i \leftarrow \text{Sig.Sign}(sk_u, h_i)$$

$$r_1, \dots, r_n \leftarrow \text{SS.Split}(d_1)$$

$$\text{Sig.Verif}(pk_u, \sigma_i, h_i,)$$

$$y_i \leftarrow \text{PKE.Dec}(sk_i, h_i)$$

$$\text{store } r_i, y_i$$

	#Users	Proxy model	#Collusions	Secrecy	Integrity	Authentication authority
PRZT+	1	Malicious	k-1	✓	✓	✓

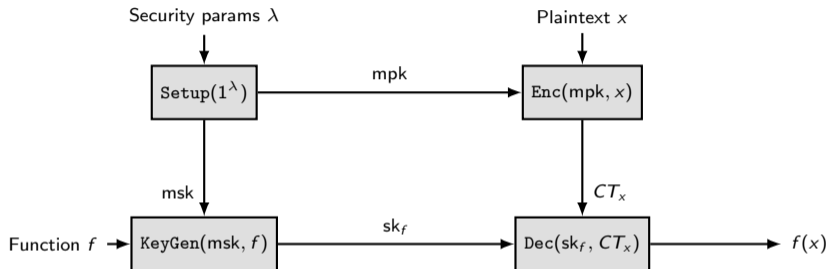
X: additional computation for the client.

FEZT: Functional Encryption-based Protocol

scheme	#Users	Proxy model	#Collusions	Secrecy	Integrity
<i>PRZT</i>	1	Honest but Curious	0	✓	✓
<i>MKZT</i>	1	Honest but Curious	k-1	✓	✓
<i>PRZT</i> +	1	Malicious	k-1	✓	✓
<i>FEZT</i>	1	Malicious	k-1	✓	✓

Primitive	Introduced	Algorithms
Functional Encryption (FE)		Setup, KeyGen, Enc, Dec
Secret Sharing (SS)	✓	Split, Merge
Asymmetric Encryption (PKE)	✓	KeyGen, Enc, Dec
AONT	✓	Hide, Rec

Functional Encryption (FE)



Notions

We denote the Functional Encryption scheme by $\{\text{Setup}, \text{KeyGen}, \text{Enc}, \text{Dec}\}$

$$(\text{mpk}, \text{msk}) \leftarrow \text{Setup}(1^\lambda),$$

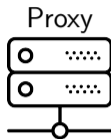
$$\text{sk}_f \leftarrow \text{KeyGen}(\text{msk}, f),$$

$$CT_x \leftarrow \text{Enc}(\text{mpk}, x)$$

$$f(x) \leftarrow \text{Dec}(\text{sk}_f, CT_x)$$

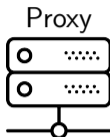
FEZT

Upload



FEZT

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$P(X), \leftarrow^{\$} \mathbb{Z}_p[X]^{k-1} \text{ st. } P(0) = 0$$

$$x_1, \dots, x_n \leftarrow^{\$} \mathbb{Z}_p^* \text{ all distincts}$$

$$r_1, \dots, r_n \leftarrow^{\$} \mathbb{Z}_p$$

$$\forall i \in [1, n], \psi_{x_i} \leftarrow \text{PKE.Enc}(x_i || r_i, pk_i)$$

Let f a polynomial s.t

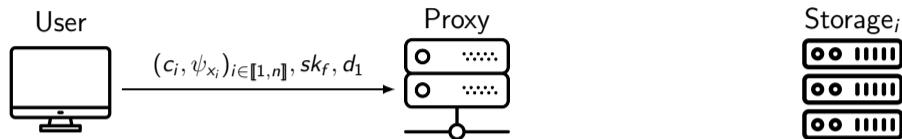
$$f(x_i || r_i || d_0) = P(x_i) + r_i + d_0$$

$$sk_f \leftarrow \text{FE.KeyGen}(f, msk)$$

$$\forall i \in [1, n], c_i \leftarrow \text{FE.Enc}(x_i || r_i || d_0, mpk)$$

FEZT

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$P(X), \stackrel{\$}{\leftarrow} \mathbb{Z}_p[X]^{k-1} \text{ st. } P(0) = 0$$

$$x_1, \dots, x_n \stackrel{\$}{\leftarrow} \mathbb{Z}_p^* \text{ all distincts}$$

$$r_1, \dots, r_n \stackrel{\$}{\leftarrow} \mathbb{Z}_p$$

$$\forall i \in [1, n], \psi_{x_i} \leftarrow \text{PKE.Enc}(x_i || r_i, pk_i)$$

Let f a polynomial s.t

$$f(x_i || r_i || d_0) = P(x_i) + r_i + d_0$$

$$sk_f \leftarrow \text{FE.KeyGen}(f, msk)$$

$$\forall i \in [1, n], c_i \leftarrow \text{FE.Enc}(x_i || r_i || d_0, mpk)$$

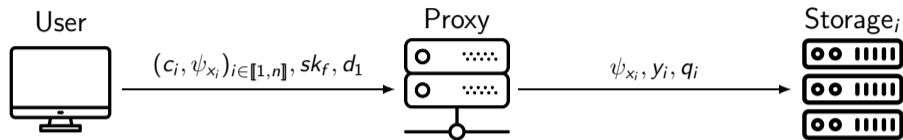
$$\forall i \in [1, n], y_i \leftarrow \text{FE.Dec}(c_i, sk_f)$$

$$(y_i = P(x_i) + r_i + d_0)$$

$$q_1, \dots, q_n \leftarrow \text{SS.Split}(d_1, n, k)$$

FEZT

Upload



$$d_0 || d_1 \leftarrow \text{AONT.Hide}(m)$$

$$P(X), \overset{\$}{\leftarrow} \mathbb{Z}_p[X]^{k-1} \text{ st. } P(0) = 0$$

$$x_1, \dots, x_n \overset{\$}{\leftarrow} \mathbb{Z}_p^* \text{ all distincts}$$

$$r_1, \dots, r_n \overset{\$}{\leftarrow} \mathbb{Z}_p$$

$$\forall i \in [1, n], \psi_{x_i} \leftarrow \text{PKE.Enc}(x_i || r_i, pk_i)$$

Let f a polynomial s.t

$$f(x_i || r_i || d_0) = P(x_i) + r_i + d_0$$

$$sk_f \leftarrow \text{FE.KeyGen}(f, msk)$$

$$\forall i \in [1, n], c_i \leftarrow \text{FE.Enc}(x_i || r_i || d_0, mpk)$$

$$\forall i \in [1, n], y_i \leftarrow \text{FE.Dec}(c_i, sk_f)$$

$$(y_i = P(x_i) + r_i + d_0)$$

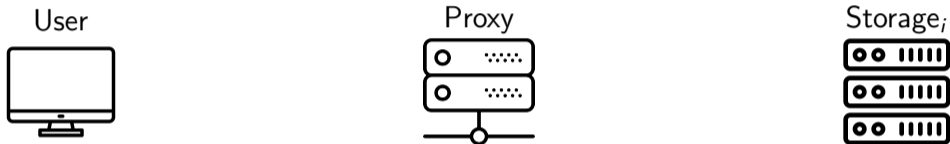
$$q_1, \dots, q_n \leftarrow \text{SS.Split}(d_1, n, k)$$

$$x_i || r_i \leftarrow \text{PKE.Dec}(\psi_{x_i}, sk_i)$$

$$\text{store } x_i, y_i - r_i, q_i$$

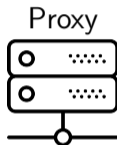
FEZT

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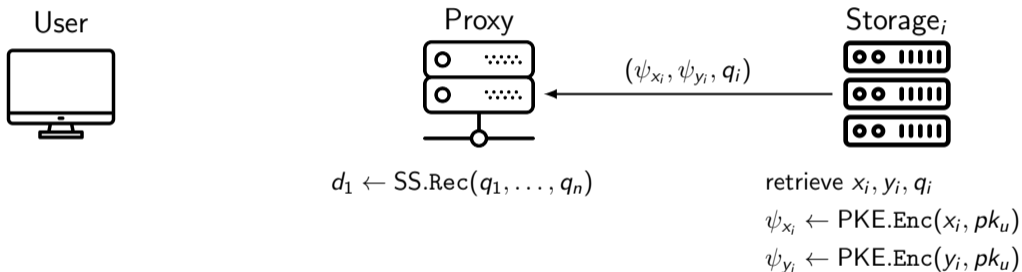
FEST

Download

retrieve x_i, y_i, q_i $\psi_{x_i} \leftarrow \text{PKE.Enc}(x_i, pk_u)$ $\psi_{y_i} \leftarrow \text{PKE.Enc}(y_i, pk_u)$

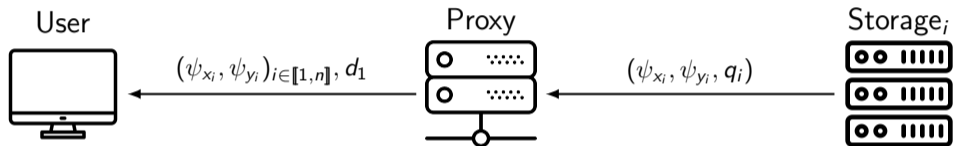
FEST

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FZT

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$$x_i \leftarrow \text{PKE.Dec}(\psi_{x_i}, sk_u)_{i \in [1, n]}$$

$$y_i \leftarrow \text{PKE.Dec}(\psi_{y_i}, sk_u)_{i \in [1, n]}$$

$$d_0 \leftarrow \text{SS.Rec}((x_i, y_i)_{i \in [1, n]})$$

$$m \leftarrow \text{AONT.Rec}(d_0 || d_1)$$

$$d_1 \leftarrow \text{SS.Rec}(q_1, \dots, q_n)$$

retrieve x_i, y_i, q_i

$$\psi_{x_i} \leftarrow \text{PKE.Enc}(x_i, pk_u)$$

$$\psi_{y_i} \leftarrow \text{PKE.Enc}(y_i, pk_u)$$

Functional Encryption

Pros and cons

scheme	#Users	Proxy model	#Collusions	Secrecy	Integrity	Authentication authority
FE	1	Malicious	k-1	✓	✓	✓

PALAFOUR: Attribute-based Protocol

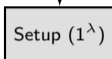
scheme	#Users	Proxy model	#Collusions	Secrecy	Integrity
<i>PRZT</i>	1	Honest but Curious	0	✓	✓
<i>MKZT</i>	1	Honest but Curious	k-1	✓	✓
<i>PRZT+</i>	1	Malicious	k-1	✓	✓
<i>FEZT</i>	1	Malicious	k-1	✓	✓
<i>PALAFOUR</i>	>1	Malicious	n	✓	✓

Primitive	Introduced	Algorithms
Secret Sharing (SS)	✓	Split, Merge
Symmetric Encryption (Sym)	✓	KeyGen, Enc, Dec
Attribute-Based Encryption (ABE)		Setup, KeyGen, Enc, Dec
Identity-Based Signature (IBS)		Setup, KeyGen, Sign, Verif

Attribute Based Encryption (ABE)

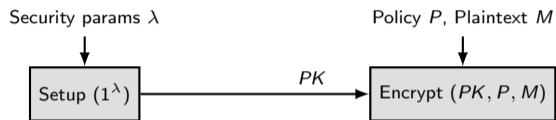
Ciphertext Policy ABE

Security params λ



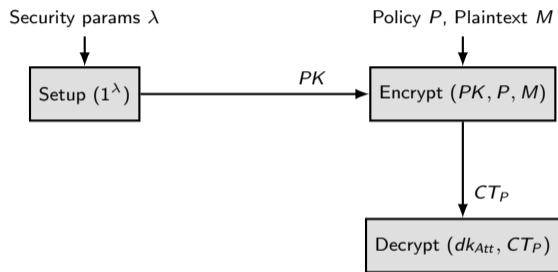
Attribute Based Encryption (ABE)

Ciphertext Policy ABE



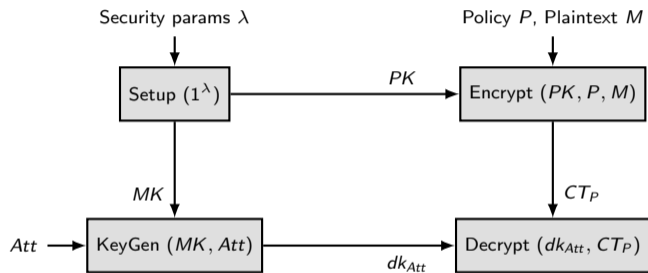
Attribute Based Encryption (ABE)

Ciphertext Policy ABE



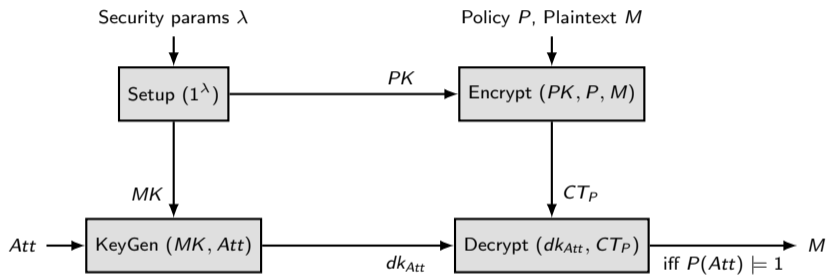
Attribute Based Encryption (ABE)

Ciphertext Policy ABE



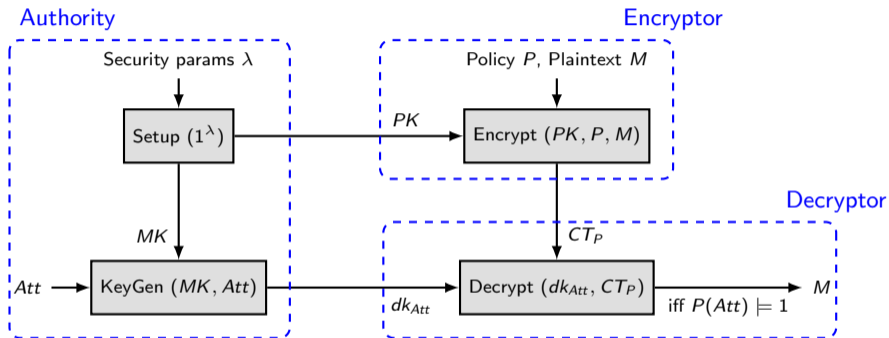
Attribute Based Encryption (ABE)

Ciphertext Policy ABE



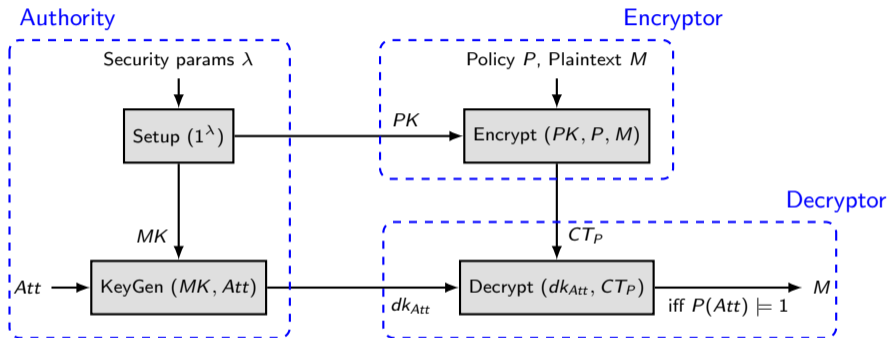
Attribute Based Encryption (ABE)

Ciphertext Policy ABE



Attribute Based Encryption (ABE)

Ciphertext Policy ABE



Notions

We denote the ABE scheme by $ABE = \{Setup, KeyGen, Enc, Dec\}$

$$PK_{ABE}, MK_{ABE} \leftarrow ABE.Setup(1^\lambda),$$

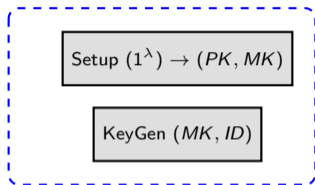
$$dk_{ABE}^{Att} \leftarrow ABE.KeyGen(MK_{ABE}, Att),$$

$$C_P \leftarrow ABE.Enc(PK_{ABE}, P, M)$$

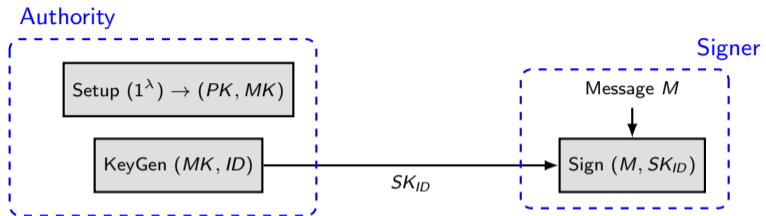
$$ABE.Dec(dk_{ABE}^{Att}, C_P)$$

Identity Based Signature (IBS)

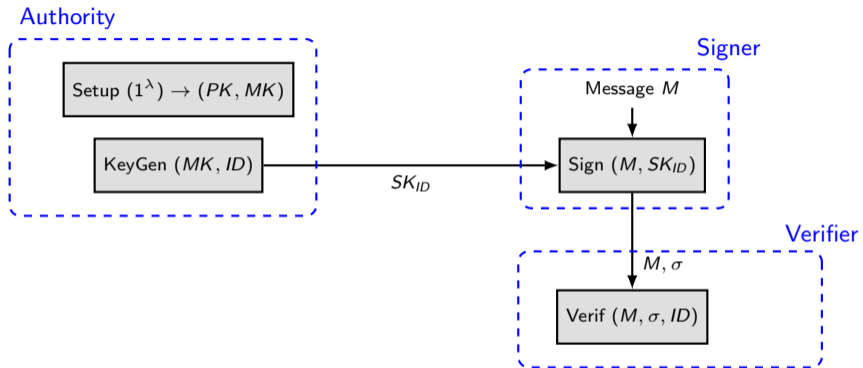
Authority



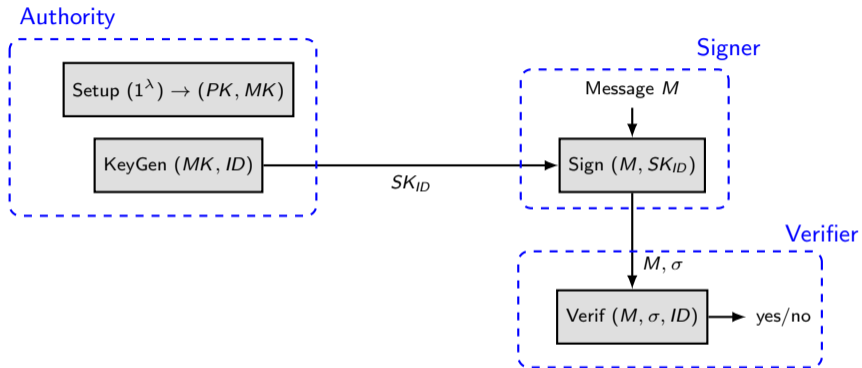
Identity Based Signature (IBS)



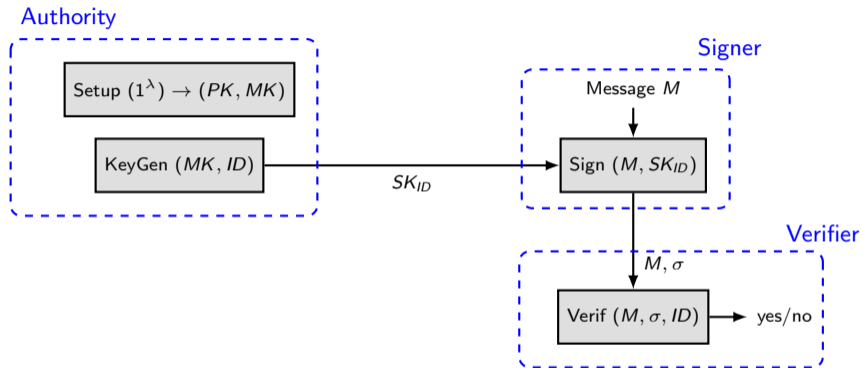
Identity Based Signature (IBS)



Identity Based Signature (IBS)



Identity Based Signature (IBS)



Notions

We denote the IBS scheme by $IBS = \{\text{Setup}, \text{KeyGen}, \text{Sign}, \text{Verif}\}$

$$PK_{IBS}, MK_{IBS} \leftarrow IBS.\text{Setup}(1^\lambda),$$

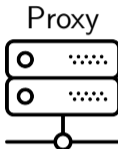
$$M, \sigma \leftarrow IBS.\text{Sign}(M, SK_{IBS}^{ID}),$$

$$SK_{IBS}^{ID} \leftarrow IBS.\text{KeyGen}(MK_{IBS}, ID)$$

$$IBS.\text{Verif}(M, \sigma, ID)$$

PALAFOUR

Upload



$$SK_{ID}^{IBS} \leftarrow \text{IBS.KeyGen}(MK, ID)$$

$$K \leftarrow \text{Sym.KeyGen}()$$

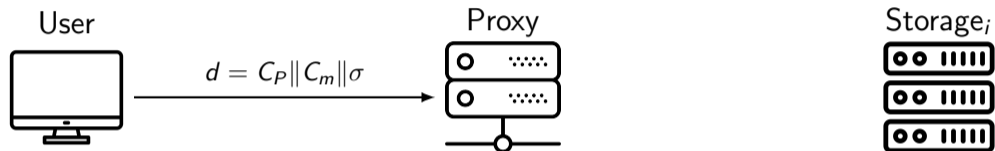
$$C_p \leftarrow \text{ABE.Enc}(PK_{\text{ABE}}, P)$$

$$C_m \leftarrow \text{Sym.Enc}(m, K)$$

$$\sigma \leftarrow \text{IBS.Sign}(C_p \| C_m, SK_{ID}^{IBS})$$

PALAFOUR

Upload



$$SK_{ID}^{IBS} \leftarrow \text{IBS.KeyGen}(MK, ID)$$

$$K \leftarrow \text{Sym.KeyGen}()$$

$$C_p \leftarrow \text{ABE.Enc}(PK_{\text{ABE}}, P)$$

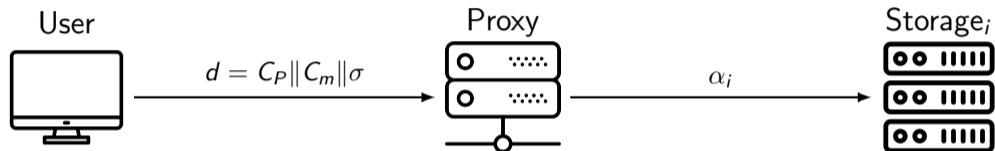
$$C_m \leftarrow \text{Sym.Enc}(m, K)$$

$$\sigma \leftarrow \text{IBS.Sign}(C_p || C_m, SK_{ID}^{IBS})$$

$$\alpha_1, \dots, \alpha_n \leftarrow \text{SS.Split}(d, n, k)$$

PALAFOUR

Upload



$$SK_{ID}^{IBS} \leftarrow IBS.KeyGen(MK, ID)$$

$$K \leftarrow Sym.KeyGen()$$

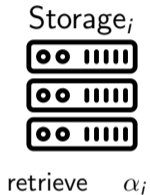
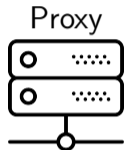
$$C_p \leftarrow ABE.Enc(PK_{ABE}, P)$$

$$C_m \leftarrow Sym.Enc(m, K)$$

$$\sigma \leftarrow IBS.Sign(C_P || C_m, SK_{ID}^{IBS})$$

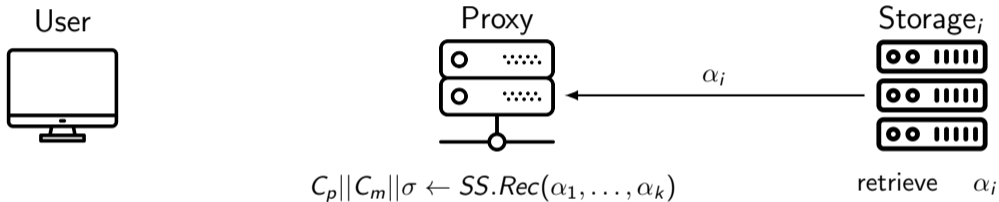
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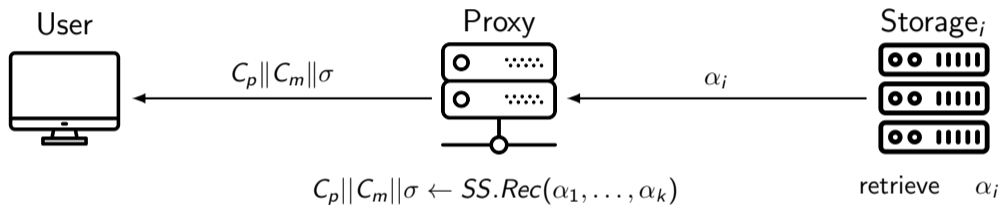
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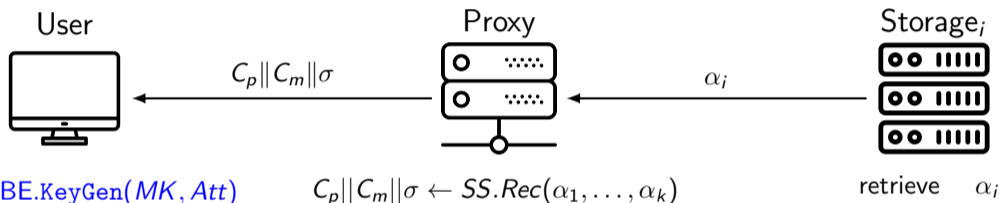
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$$dk_{Att}^{ABE} \leftarrow \text{ABE.KeyGen}(MK, Att)$$

$$\text{IBS.Verif}(\sigma, ID) \models 1$$

$$K \leftarrow \text{ABE.Dec}(C_p, dk_{Att}^{ABE})$$

$$m \leftarrow \text{Sym.Dec}(C_m, K)$$

$$C_p || C_m || \sigma \leftarrow \text{SS.Rec}(\alpha_1, \dots, \alpha_k)$$

retrieve α_j

Instances

Ciphertext-Policy Attribute-Based Encryption (CP-ABE) [Wat11]

- Elliptic curve, pairing-based
- Expressive
- Efficient
- Implemented by OpenABE [Zeu]

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- Elliptic curve, pairing-based
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- Efficient
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Identity-Based Signature (IBS) [BB04]

- Elliptic curve, pairing-based
- Short signature
- Efficient
- Implemented by RELIC [AGM+]

Comparison

scheme	#Users	Proxy model	#Collusions	Secrecy	Integrity
<i>PRZT</i>	1	Honest but Curious	0	✓	✓
<i>MKZT</i>	1	Honest but Curious	k-1	✓	✓
<i>PRZT</i> +	1	Malicious	k-1	✓	✓
<i>FEZT</i>	1	Malicious	k-1	✓	✓
<i>PALAFOUR</i>	>1	Malicious	n	✓	✓

Comparison

Scheme		Messages exchanges	
		Client ↔ Proxy	Proxy ↔ one Provider
<i>PRZT</i>	Upload	$ m + PRE\ cipher $	$\frac{ m }{k} + PRE\ cipher $
	Download	$ m + PRE\ cipher $	$\frac{ m }{k} + PRE\ cipher $
<i>MKZT</i>	Upload	$ m + MKE\ cipher $	$\frac{ m }{k} + 3 * (n - 1) * MKE\ cipher $
	Download	$ m + MKE\ cipher $	$\frac{ m }{k} + MKE\ cipher $
<i>PRZT</i> +	Upload	$ m + n * Asym\ cipher + n * Asymsignature $	$\frac{ m }{k} + Asym\ cipher + Asymsignature $
	Download	$ m + n * nonce\ Asym\ cipher + n * Asym\ cipher $	$\frac{ m }{k} + nonce\ Asym\ cipher + Asym\ cipher $
<i>FEZT</i>	Upload	$ m + n * FE\ cipher + n * Asym\ Cipher + FE\ function\ key $	$\frac{ m }{k} + Asym\ Cipher + C $
	Download	$ m + n * FE\ cipher + 2 * Asym\ Cipher $	$\frac{ m }{k} + 2 * Asym\ Cipher $
<i>PALAFOUR</i>	Upload	$ signature\ IBS + C * (policy\ size) + m = d$	$\frac{d}{k}$
	Download		

Conclusion

Contributions

- 1 Attack on *PRZT*

Conclusion

Contributions

- 1 Attack on *PRZT*
- 2 Attacks on *MKZT*

Conclusion

Contributions

- 1 Attack on *PRZT*
- 2 Attacks on *MKZT*
- *PRZT+*

Conclusion

Contributions

- 1 Attack on *PRZT*
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- *PRZT*+
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- *FEZT*
- *PALAFOUR*

Conclusion

Contributions

- 1 Attack on *PRZT*
- 2 Attacks on *MKZT*
- *PRZT*+
- *FEZT*
- *PALAFOUR*

Future Work

- Post-Quantum

Conclusion

Contributions

- 1 Attack on *PRZT*
- 2 Attacks on *MKZT*
- *PRZT*+
- *FEZT*
- *PALAFOUR*

Future Work

- Post-Quantum
- Authority removal

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